



P.E.S. College of Engineering, Mandya - 571 401

(An Autonomous Institution affiliated to VTU, Belgaum)

Fourth Semester, B.E. - Electrical and Electronics Engineering

Semester End Examination; June/July - 2015

Signals and Systems

Time: 3 hrs

Max. Marks: 100

Note: i) Answer **FIVE** full questions, selecting **ONE** full question from each **Unit**.
 ii) Assume suitable missing data if any.

UNIT - I

1. a. Determine the periodicity of the continuous signal given by

$$x(t) = 2 \cos \frac{2\pi t}{3} + 3 \cos \frac{2\pi t}{7} \text{ and prove the same.}$$

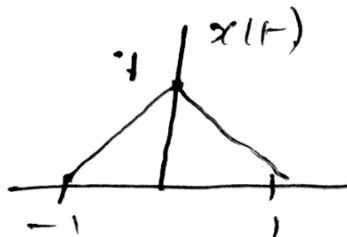
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b. Determine the even and odd parts of $x(t) = \sin 2t + \cos t + \sin t \cos 2t$

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c. A triangular pulse $x(t)$ is shown below. Sketch (i) $y_1(t) = x(2t)$ (ii) $y_2(t) = x(-2t-1)$

(iii) $y_3(t) = x[2(t-2)]$



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2 a. Determine the power and Energy of the $x(t) = 3 \cos 5\Omega_0 t$

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b. For the system given by $y(n) = \sum_{k=n_0}^n x(k)$ determine, whether the system is (i) memory less

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(ii) linear (iii) Time in variant

(iv) Casual (v) Stable

c. Plot the standard continuous time signals. Write the functional relations of each of it.

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UNIT - II

3 a. Perform the convolution of the following signals by graphical method. $x_1(t) = e^{-3t}u(t)$,

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$$x_2(t) = t u(t).$$

b. Determine the linear convolution of the function:

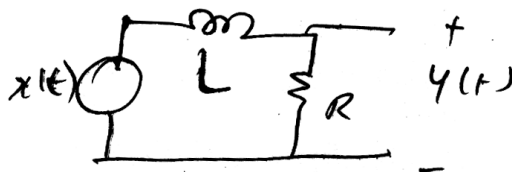
$$x(n) = \begin{cases} 1 & \text{for } n = \pm 1 \\ 2 & \text{for } n = 0 \\ 0, & \text{otherwise} \end{cases} \quad h(n) = \begin{cases} 2 & n = 0 \\ 3 & n = 1 \\ -2 & n = 2 \\ 0 & \text{otherwise} \end{cases}$$

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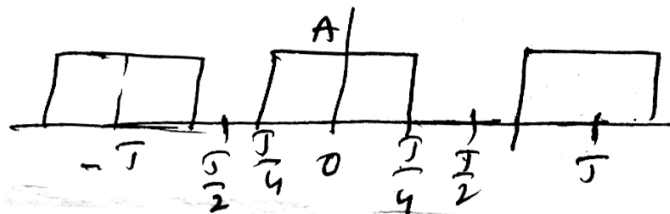
- 4 a. A LTI system has impulse response given by $h(n) = u(n) - u(n-7)$. Determine the output of the system when the input is $x(n) = 2[u(n-2) - u(n-5)]$. 10
- b. Consider the linear Time variant system with impulse response $h(n) = \left[\frac{j}{2}\right]^n u(n)$. Determine the steady state response for large n, to the excitation $x(n) = \cos \pi n u(n)$ 10

UNIT - III

- 5 a. Find the zero-input response and zero-state response and hence find total response of the functions given by $\frac{d^2 y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 4y(t) = \frac{d}{dt} x(t)$ 8
 given by $y(0) = 0, \left. \frac{dy(t)}{dt} \right|_{t=0} = 1 \quad x(t) = e^{-2t} u(t)$
- b. Draw the direct form I and direct form II block diagram representatives of the system described by $\frac{d^2 y(t)}{dt^2} + 2 \frac{dy(t)}{dt} + 3y(t) = 4 \frac{dx(t)}{dt} + 5x(t)$. 6
- c. What are the conditions to be satisfied for the Fourier representation of a signal? Write the three forms of CTFS of periodic signal. 6
6. a The impulse response of the circuit shown is $h(t) = \frac{R}{L} e^{-\left(\frac{R}{L}\right)t} u(t)$. Find the expression for the frequency response and plot the magnitude of phase response. 10



- b. Determine the trigonometric form of Fourier series of the wave forms.



UNIT - IV

- 7 a. State and prove linearity time shifting, frequency shifting and symmetry property of DTFT. 10

- b. Use partial fractions expansion and linearity to determine the inverse Fourier transfer in the following functions.

$$(i) x(jw) = \frac{-jw}{(jw)^2 + 3jw + 2} \quad (ii) x(jw) = \frac{4}{-w^2 + 4jw + 3}$$

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- 8 a. Find the DTFT of the following finite durations sequence of length L.

$$x(n) = \begin{cases} A & \text{for } 0 \leq n \leq L-1 \\ 0 & \text{otherwise} \end{cases} \text{ also find the inverse DTFT to verify } x(n) \text{ for } L = 3 \text{ and}$$

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A = 1 V.

- b. Determine the IDFT of $x(n) = \{3, (2 + j), 1, (2 - j)\}$

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UNIT - V

- 9 a. Find the initial value $x(0)$ and final value $x(\infty)$ of the following Z- domain

$$(i) X(z) = \frac{1}{1 - z^{-2}} \quad (ii) X(z) = \frac{2z}{z^2 - 1.8z + 0.8}$$

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- b. Find the one sided Z-transform of the discrete time signal generates by mathematically simplify of Cartesians time signal $x(t) = e^{-at} \sin \Omega_o t$

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- c. Find the Z-transform of the following sequences (i) $x(n) = 3\left(\frac{1}{2}\right)^n u(n) - 2(3)^n u(-n-1)$

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$$(ii) x(n) = \left(\frac{1}{2}\right)^n [u(n) - u(n-10)] \text{ Write Time shifting property and linearity property.}$$

- 10 a. Determine the IZT of $X(z) = \frac{1}{1 - 1.5z^{-1} + 0.5z^{-2}}$ for ROC $|z| > 1, \frac{1}{2} < |z| < 1, |z| < \frac{1}{2}$

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- b. The impulse response of a discrete line LTI system is given by

$$h(n) = \left(\frac{1}{2}\right)^n u(n) + \left(-\frac{1}{3}\right)^n u(n) \text{ Find the Z-transform of } h(n) \text{ and its ROC and hence find}$$

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(i) is the system casual or non-casual

(ii) is the system is stable

(iii) Obtain the difference equation realization of the system.

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