

b. Show that the transfer function  $\frac{U(S)}{E(S)}$  of the PID controller shown in Fig. 3b is,

$$\frac{U(S)}{E(S)} = K_0 \frac{T_1 + T_2}{T_1} \left[ 1 + \frac{1}{(T_1 + T_2)S} + \frac{T_1T_2S}{T_1 + T_2} \right] \text{ Assume K} >> 1$$

$$10$$

$$V_{K_0} = \frac{T_1S}{1 + T_1S} + \frac{1}{(T_1 + T_2)S} + \frac{T_1T_2S}{T_1 + T_2} \right] K_{K_0} = \frac{1}{1 + T_1S} + \frac{1}{(T_1 + T_2)S} + \frac{1}{(T_1 + T_2)S}$$

4. A unity feedback system with  $G(S) = \frac{4}{(S+1)(S+2)}$  will have a phase margin of 50° at a

20 frequency of 1.7 rad/sec. Design a PI controller and explain the effects and performance and stability of a system by drawing Bode diagram for both the cases (without and with controllers).

## **UNIT - III**

- 5 a. Discuss the effects and limitations of LAG compensators.
- b. Explain the behaviour in terms of unit step and ramp response curves for uncompensated and compensated (LAG, LEAD, LAG-LEAD) systems.

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6. Design a lead compensator for a system whose open loop transfer function is

:

$$G(S) = \frac{10}{S(S+6)}$$
. It will fulfill the following requirements

(i) Static velocity error constant  $K_v = 20 \text{ sec}^{-1}$ 

(ii) Phase margin is at atleast 50°

(iii) Gain margin is atleast 10 db.

Draw the Bode diagram only for the uncompensated system and determine the compensator transfer function.

## UNIT - IV

- 7 a. Explain the control system design via pole placement technique by state feedback and 10 determine the state feedback gain matrix 'K' by any one method.
- b. Determine the State feedback gain matrix 'K' by using Ackermann's formula for the regulator

system 
$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ -1 & -5 & -6 \end{bmatrix}$$
,  $B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$  with  $u = -Kx$  choose the closed loop poles at 10  
 $S = -2 + i4$ ,  $S = -2 - i4$  and  $S = -10$ .

8 a. Design a type 1 servo system when the plant transfer function has an integrator. Assume that

the plant transfer function is given by, 
$$\frac{Y(S)}{U(S)} = \frac{1}{S(S+1)(S+2)}$$
. 10

The desired closed loop poles are  $S = -2 \pm i 2\sqrt{3}$  and S = -10. Assume that the reference input is a step function. Obtain the unit step response of the designed system.

b. Explain how to design type 1 servo system when the plant has no integrator.

## UNIT - V

9 a. What is the state observer and explain the need for state observer. Explain the different 10 methods of evaluating the state observer gain matrix Ke.

b. For the system 
$$\dot{X} = Ax + bu$$
,  $Y = Cx$ , where  $A = \begin{bmatrix} 0 & 20.6 \\ 1 & 0 \end{bmatrix}$ ,  $B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$ ;  $C = \begin{bmatrix} 0 & 1 \end{bmatrix}$  use  
10

 $u = -K\hat{X}$ . Design a full order observer, if the desired Eigen values of the observer matrix are  $\mu_1 = -10$ ,  $\mu_2 = -10$  (Use Ackermann's formula).

- 10 a. Write a note on Quadratic optimal regulator system with Riccatti equation. 10
  - b. Determine the optimal feedback gain matrix K for the performance index J to minimize for

$$A = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}, B = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \& Q = \begin{bmatrix} 1 & 0 \\ 0 & \mu \end{bmatrix}, \text{ where } \mu \ge 0 \text{ for the float } \dot{X} = Ax + Bu, \text{ with the use } 10$$

of reduced matrix Riccatti equation in the design of optimal control system.

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