



**P.E.S. College of Engineering, Mandya - 571 401**

(An Autonomous Institution affiliated to VTU, Belgaum)

First Semester, M. Tech - Civil Engineering (MCAD)

Semester End Examination; Jan - 2017

Computational Structural Mechanics

Time: 3 hrs

Max. Marks: 100

Note: Answer FIVE full questions, selecting ONE full question from each unit.

**UNIT - I**

- 1 a. Explain the concepts of flexibility and stiffness methods of matrix analysis. 8
- b. Discuss how to determine the static and kinematic indeterminacy of pin-jointed plane truss. 6
- c. Explain : 6
  - i) Local axis                      ii) Global axes                      iii) Rotation transformation matrix.
- 2. Analyze the pin-jointed plane truss shown in Fig. Q2, by direct stiffness method. 20  
 Take  $A = 100 \text{ mm}^2$  and  $E = 200 \text{ GPa}$  for all members.

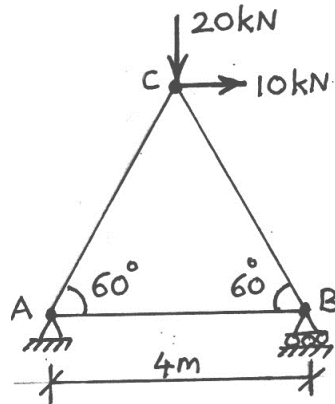


Fig. Q2

**UNIT - II**

- 3. Analyze the continuous beam shown in Fig. Q3, by direct stiffness method. Sketch neatly the BMD, and SFD. Assume  $EI = 48,000 \text{ kN-m}^2$ . 20

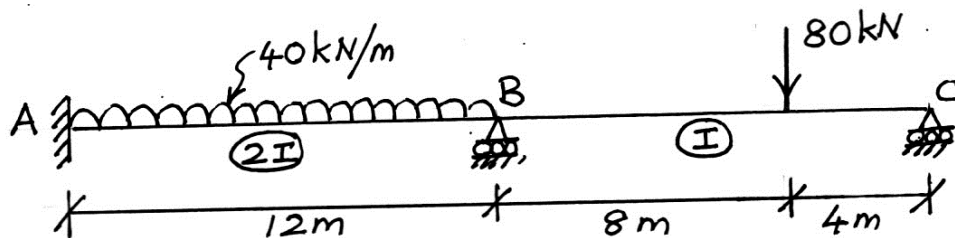
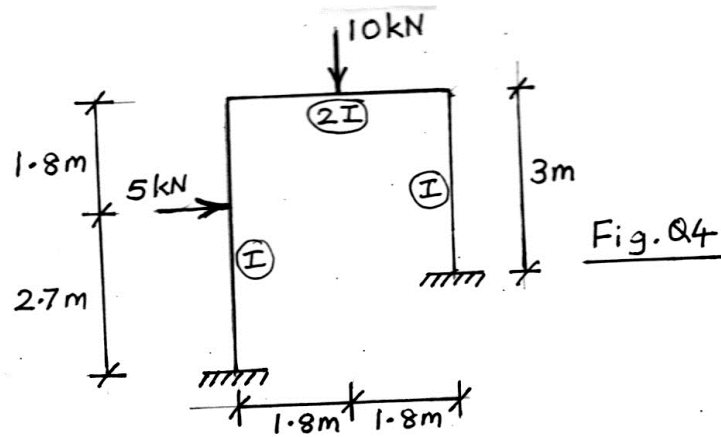


Fig. Q3

- 4. Analyze the rigid-jointed plane frame shown in Fig. Q4, by direct stiffness method. Sketch neatly the BMD. 20

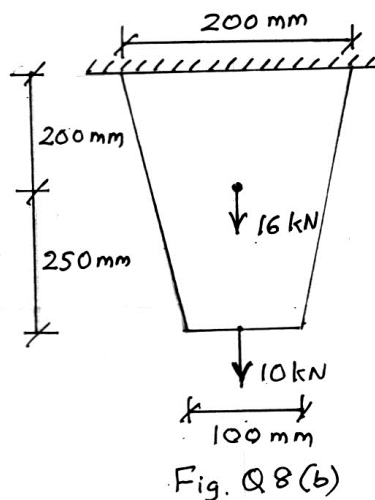


UNIT - III

- 5 a. List the advantages of finite element method. 5
- b. State and explain the principle of minimum potential energy. 5
- c. Explain the important steps in finite element analysis. 10
- 6 a. Discuss on 'the choice of displacement function' in finite element analysis. 6
- b. Discuss the concept of weighted residual method. 8
- c. What are natural coordinates? Explain its importance. 6

UNIT - IV

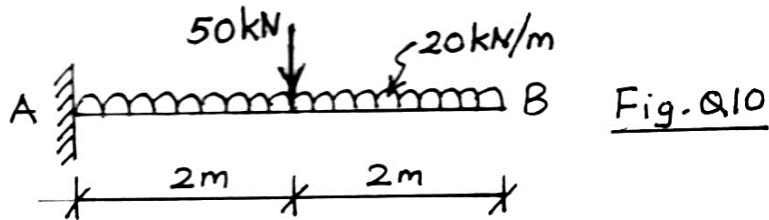
- 7 a. Obtain the shape functions for a two-noded bar element using Lagrange interpolation formula. 5  
 Also sketch neatly the shape functions.
- b. Derive the expression of equivalent nodal body force vector for a three-noded bar element. 8
- c. Derive the stiffness matrix for a two-noded bar element. 7
- 8 a. What are isoparametric elements? Discuss with a suitable example. 5
- b. A circular tapering bar carries loads as shown in Fig. Q8(b). It also carries a tractive force 6 kN/m. The weight density is 78 kN/m<sup>3</sup>. Idealise the bar as two 2-noded bar elements. Find the stresses in the two elements. Take E = 200 GPa.



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## UNIT - V

- 9 a. Sketch neatly a beam element showing the DOFs. Write the stiffness matrix of the beam element (Do not derive). 4
- b. Explain consistent nodal loads with an example. 4
- c. Derive the shape functions for a two-noded beam element. Also plot neatly the variation of the shape functions. 12
10. Analyze the cantilever beam shown in Fig. Q10, by finite element analysis.  
Take  $EI = 40,000 \text{ kN-m}^2$ . Sketch BMD, elastic curve and SFD.



20

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