



P.E.S. College of Engineering, Mandya - 571 401

(An Autonomous Institution affiliated to VTU, Belgaum)

First Semester, M. Tech - Mechanical Engineering (MMDN)

Make – up Examination; Feb - 2016

Finite Element Methods

Time: 3 hrs

Max. Marks: 100

Note: Answer FIVE full questions, selecting ONE full question from each unit.

UNIT - I

- 1 a. Differentiate between the following :
 - i) Global and Local Coordinate systems 9
 - ii) Essential and Natural Boundary Conditions.
- b. Highlight the rules to guide the placement of nodes when obtaining approximate solution to differential equation. 6
- c. What is shape function? List the characteristics of shape functions. 5
- 2 a. Derive shape functions for quadratic bar element and plot the variation of shape functions along the length of the element. 8
- b. For the composite structure of axially loaded member shown in Fig. 2(b). Find unknown displacement and Reaction forces. 12

UNIT - II

- 3 a. Show that shape function for Linear Quadrilateral element is given by

$$N_i = \frac{1}{4}(1 + \xi\xi_i)(1 + \eta\eta_i)$$
8

Where $i = 1, 2, 3, 4$.
- b. For a Linear triangular element,

$$N_1 = \frac{1}{16}(40 - 3x - 4y)$$

$$N_2 = \frac{1}{16}(-16 + 4x)$$

$$N_3 = \frac{1}{16}(-8 - x + 4y)$$
12

And $\mu = 0.3$ E = 2 10^5 MPa out $t_e = 1$. Determine the strain displacement matrix and stiffness matrix for a plane strain element.
- 4 a. Using Lagrange functions derive shape function for hexahedron (Brick) element. 8
- b. Differentiate between CST and LST element. 4
- c. Evaluate the Jacobian matrix at the local coordinates $\xi = \eta = 0.5$ for the linear quadrilateral element with its global coordinates at (4, 4), (7, 5), (8, 10) and (3, 8) at nodes 1, 2, 3 and 4 respectively. 8

UNIT - III

- 5 a. What is meant by axi-symmetric field problem? Give example. List the required conditions for a problem assumed to be axi-symmetric and also write down the relationship between stress and strain for the axi-symmetric problem. 10
- b. Derive [B] matrix for an axi-symmetric triangular element. 10
6. For the three bar truss shown in Fig. Q. 6(a) determine the nodal displacements and the – stresses in each member. Find the support reactions also. 20
Take $E = 200 \text{ GPa}$, $A_1 = 1500 \text{ mm}^2$ and $A_2 = A_3 = 2000 \text{ mm}^2$.

UNIT - IV

- 7 a. Differentiate between Lagrange's and Hermit interpolation function. 4
- b. Find the deflection and slopes at the nodes for the aluminium beam shown in Fig. Q. 7(b). 16
- 8 a. Derive the mass matrix for a 2 noded one dimensional bar element. 6
- b. For the bar shown in Fig. Q8(b) determine the first two natural frequencies. 14
Take $E = 210 \text{ GPa}$, $\rho = 7860 \text{ kg/m}^3$ $A_1 = A_2 = 650 \text{ mm}^2$. Use lumped mass matrix equations.

UNIT - V

- 9 a. Consider a wall of a tank containing a hot liquid at a temperature T_o with an air stream of temperature T_∞ passed on the outside maintaining a wall temperature of T_w at the boundary specify the governing differential equation for one dimensional heat conduction and specify the boundary conditions. 4
- b. A composite slab consists of three materials with thermal conductivities of $20 \text{ W/m}^\circ\text{C}$, $30 \text{ W/m}^\circ\text{C}$, $50 \text{ W/m}^\circ\text{C}$ and thickness of 0.3 m , 0.15 m and 0.15 m respectively. The outer surface is at 20°C and the inner surface is exposed to the convective heat transfer coefficient of $25 \text{ W/m}^2\text{C}$ and a medium at 800°C . Determine the temperature distribution within the wall. 16
- 10 a. Derive element conductivity matrix for a 1D heat conduction problem using Galerkin approach. 6
- b. Calculate the temperature distribution in a one dimensional fin with the physical properties given in Fig. Q.10 (b). The fin is rectangular in shape and is 8 cm long, 4 cm wide and 1 cm thick. Assume that convection heat loss occurs from the fin. Model the fin by four elements. 14

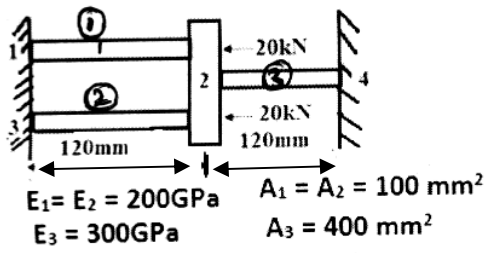


Fig. Q 2 (b)

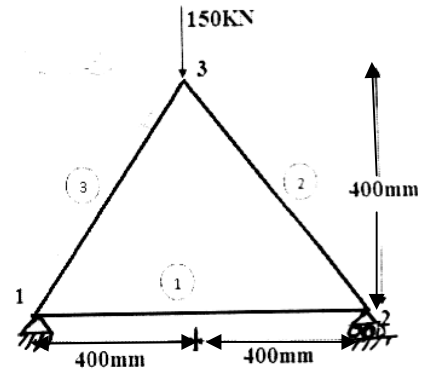


Fig. Q 6.

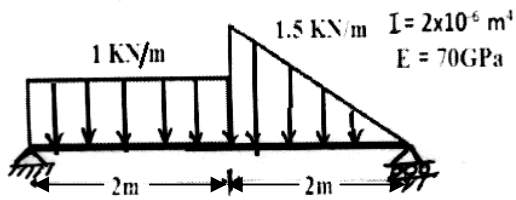


Fig. Q 7 (b)

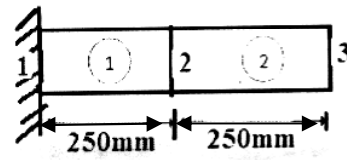


Fig. Q 8 (b)

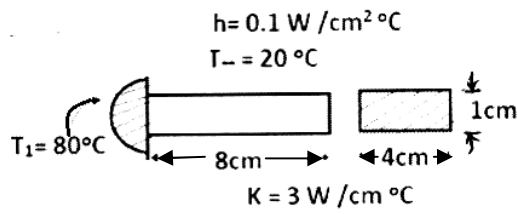


Fig. Q 10 (b)
