



P.E.S. College of Engineering, Mandya - 571 401
 (An Autonomous Institution affiliated to VTU, Belagavi)
Eighth Semester, B.E. - Electrical and Electronics Engineering
Semester End Examination; June - 2017
Discrete Time Control System

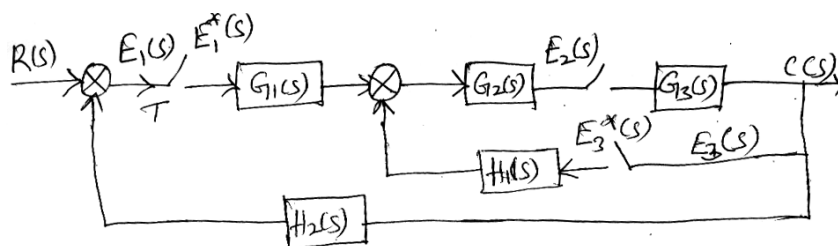
Time: 3 hrs

Max. Marks: 100

Note: Answer FIVE full questions, selecting ONE full question from each unit.

UNIT - I

- 1 a. What are the advantages of Discrete Time Control System over a Continuous Time Control Systems? 10
- b. With block diagram, explain the practical circuit of Sample and Hold circuit. 10
- 2 a. What are the properties of Z-transformation? Prove any two of them. 10
- b. Consider the multi-loop multi-sampler digital control system shown in below figure. Find the closed-loop transfer function for this system.



UNIT - II

- 3 a. Explain the mapping between S-plane to Z-plane. 8
- b. Explain the different methods available for checking the stability of sampled data control systems. 12
- 4 a. The characteristic equation of a sampled data system is given by :
 $Z^4 - 0.9Z^3 + 0.14Z^2 + 0.216Z + 0.03Z = 0$ 12
 By Jurg's test investigate the stability of the system and verify the result by the method of bilinear transformation.
- b. Explain static and steady state error constants of DTCS. 8

UNIT - III

- 5 a. Define the following with respect to state space analysis : 8
 - i) State
 - ii) State variable
 - iii) State vector
 - iv) State space.

b. Pulse transfer function of a system to is given by:

$$\frac{Y(Z)}{u(Z)} = \frac{3Z}{(Z+1)^2(2Z+1)} \quad 12$$

Obtain the state model realization in,

i) Controllable canonical form ii) Observable canonical form.

6 a. State all the properties of state transition matrix (STM). 8

b. A discrete-time system is represented by the state model :

$$x(k+1) = \begin{bmatrix} 0 & 1 \\ -0.16 & 1 \end{bmatrix} x(k) + \begin{bmatrix} 1 \\ 1 \end{bmatrix} r(k)$$

$$y(k) = [1 \quad 0]x(k), \quad x(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \quad 12$$

Determine a discrete-unit step response of the system, also obtain the pulse transfer function.

UNIT - IV

7 a. Determine whether or not the following quadratic form is negative definiteness. 10

$$Q = -x_1^2 - 3x_2^2 - 11x_3^2 + 2x_1x_2 - 4x_2x_3 - 2x_1x_3$$

b. Explain the Liapunov stability analysis for linear time invariant continuous time systems. 10

8 a. Consider a second – order autonomous system given by

$$x_1(k+1) = x_2(k), \quad x_2(k+1) = 5x_1(k) - 8x_2(k) \quad 12$$

Generate a Liapunov function and investigate stability of the system.

b. Explain asymptotic stability, stability in large and instability. 8

UNIT - V

9 a. Explain state controllability and observability with Kalman’s test. 10

b. Explain the principle of duality. 10

10a. Consider a system is described by,

$$F = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -5 & -6 \end{bmatrix}; G = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \quad 12$$

Using state feedback control $u(k) = -k x(k)$,

It is desired to have poles at $Z = -0.2 \pm j0.5$ and $Z = -0.8$, determine the state feedback gain matrix ‘k’.

b. Explain the design procedure for state observers. 8

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