



P.E.S. College of Engineering, Mandya - 571 401

(An Autonomous Institution affiliated to VTU, Belagavi)

Fourth Semester, B.E. - Information Science and Engineering

Semester End Examination; June - 2017

Finite Automata and Formal Languages

Time: 3 hrs

Max. Marks: 100

Note: Answer **FIVE** full questions selecting **ONE** full question from each unit.

UNIT - I

1. a Construct a DFA to accept the following

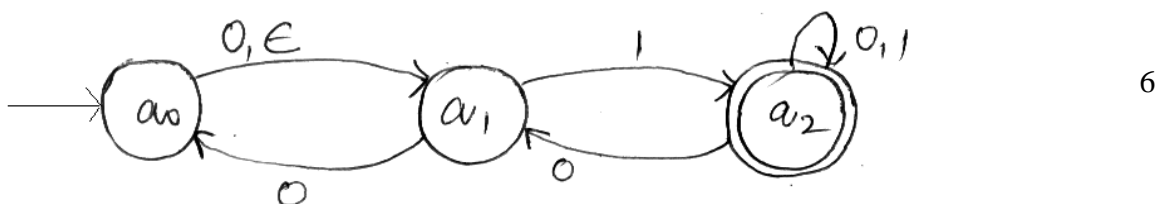
- i) Strings of 0's and 1's starting with at least two 0's ending with at least two 1's 8
- ii) Strings of a's and b's having even number a's and odd number of b's

b. Differentiate between NFA and DFA and explain the applications of Finite automata. 5

c. Convert the given NFA to DFA



2 a. Construct a DFA from the following epsilon NFA.



b. Design a DFA to accept the language

$$L = \{W(ab+ba) \mid W \in \{a,b\}^*\}$$

4

c. Find the minimized DFA for the following:

| | | |
|----|---|---|
| S | 0 | 1 |
| →A | B | A |
| B | A | C |
| C | D | B |
| *D | D | A |
| E | D | F |
| F | G | E |
| G | F | G |
| H | G | D |

10

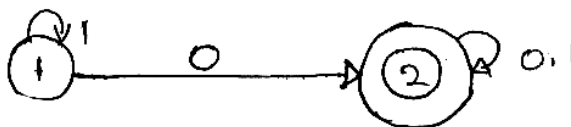
UNIT - II

3 a. Obtain the regular expression for the following languages

i) $L = \{a^n b^m : (m+n) \text{ is even}\}$ 4

ii) $L = \{a^n b^m : n > 4 \text{ and } m \leq 3\}$

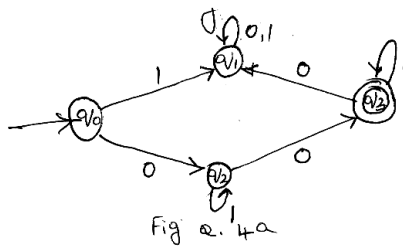
b. Obtain the regular expression from the given DFA using Kleen's theorem



c. Construct the automata for the regular expression $(a+b)(ab+ba)^*aa$ 4

d. List and explain the applications of regular expressions. 6

4 a. Obtain the regular expression for the following DFA using state elimination method.



b. State and prove pumping lemma for regular languages. 10

c. Prove that the language

$L = \{a^n / n \geq 0\}$ 7

Is not regular?

UNIT - III

5 a. Write the CFG for the following languages

i) $L = \{a^i b^j c^k : i+j = k, i, j \geq 0\}$ 5

ii) $L = \{a^n b^m c^k : n+2m = k, n, m, k \geq 0\}$

b. Obtain two leftmost & rightmost derivations for the string 'abababa' from the grammar

$S \rightarrow SbS | a$ 5

c. Write CFG for the language consist of strings of palindrome with the input symbols a and b.

Where the length of the string may be even or odd. 5

d. Show that the following grammar is ambiguous: 5

$S \rightarrow S + S | S * S | S - S | a | b | c$

6. a Remove all useless productions, unit productions and ϵ productions from the grammar

$S \rightarrow ABC | BaB \quad A \rightarrow aA | BaC | aaa \quad B \rightarrow aBa | a | D$ 10

$C \rightarrow CA | AC \quad D \rightarrow \epsilon$

- b. If L_1 and L_2 are CFL then P.T. they are closed under union and concatenation operations. 6
- c. Convert the following CFG to CNF $S \rightarrow ABa$ $A \rightarrow aab$ $B \rightarrow AC$ 4

UNIT - IV

- 7 a. Design a PDA to accept a string of balanced parenthesis and also show the string acceptance for the string $W=[()]$. 12

- b. Construct a PDA from the grammar :

$$S \rightarrow aABB / aAA$$

$$A \rightarrow aBB / a$$

$$B \rightarrow bBB / A$$

$$C \rightarrow a$$

S is a Start symbol

8

- 8 a. Construct a PDA for the language

$$L = \{WW^R \mid w \in (a+b)^*\}$$
 and show the string acceptance for the string abbbba. 12

- b. Convert the following grammar into PDA

$$S \rightarrow aSa/aa$$

$$S \rightarrow bSb/bb$$

And also show the string acceptance.

8

UNIT-V

- 9 a. Design Turing machine to accept the language having string of palindromes over $\{a, b\}$. 10
- b. Design a Turing machine to accept the language consists of equal number of 0's and 1's 10
- 10 a. Explain ID, acceptance of language with respect to Turing machine with an example. 8
- b. Explain the following:
- i) Post correspondence problem 12
 - ii) Undecidable problems
 - iii) Multi track Turing machine.

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