b. Use fourth order Runge-Kutta method to compute y(1.1), given that $\frac{dy}{dx} = xy^{\frac{1}{3}}$, y(1) = 1. 7

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c. If
$$\frac{dy}{dx} = 2e^x - y$$
, $y(0) = 2$, $y(0.1) = 2.010$, $y(0.2) = 2.040$ and $y(0.3) = 2.090$, find $y(0.4)$

correct to four decimal places by using Milne's Predictor-Corrector method.

UNIT - III

- 5 a. Find the skewness and kurtosis, if the first four moments of a frequency distribution about x = 4 are respectively 1, 4, 10 and 45.
 - b. Fit a parabola of second degree $y=ax^2+bx+c$ for the data :

x	0	1	2	3	4
У	1	1.8	1.3	2.5	2.3

c. Find the coefficient of correlation and obtain the lines of regression for the data :

x	5	7	8	10	11	13	16
у	33	30	28	20	18	16	9

6. a. A random variable x has the following Probability function for various values of x,

x	0	1	2	3	4	5	6	7
P(x)	0	k	2k	2k	3k	k ²	$2k^2$	$7k^2+k$

i) Find k

ii) P(x < 6), $P(x \ge 6)$ and $P(3 < x \le 6)$.

- b. The number of accidents in a year to taxi drivers in a city follows a Poisson distribution with mean 3. Out of 1000 taxi drivers find approximately the number of drivers with,
 i) No accident in a year
 ii) More than 3 accidents in a year.
- c. The marks of 1000 students in an examination fallows a Normal distribution with mean 70 and standard deviation 5. Find the number of students whose marks will be :

i) Less than 65 ii) More than 75 iii) Between 65 and 75. (Given $\phi(1) = 0.3413$).

UNIT - IV

7 a. Suppose X and Y are independent random variables with the following respective distribution, find the joint probability distribution of X and Y. Also verify that COV (X, Y) = 0.

Xi	1	2	y_j	-2	5	8
$f(x_i)$	0.7	0.3	$g(y_j)$	0.3	0.5	0.2

b. If the Joint probability function of the random variables X and Y is given by,

$$f(x, y) = \begin{cases} cxy, & 0 \le x \le 2 & 0 \le y \le x \\ 0, & otherwise \end{cases}$$

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Determine *c* and hence find $P\left(\frac{1}{2} < X < 1\right)$.

c. Find the unique fixed probability vector of the regular stochastic matrix,

$$P = \begin{bmatrix} 0 & 1 & 0 \\ \frac{1}{6} & \frac{1}{2} & \frac{1}{3} \\ 0 & \frac{2}{3} & \frac{1}{3} \end{bmatrix}.$$
7

8 a. Solve the system of equation by Gauss-Seidel method :

8x+3y+2z=13, 2x+y+6z=9, x+5y+z=7 starting from $[0,0,0]^{T}$ carry out four 6 iterations.

- b. Solve: 10x + 2y + z = 9, x + 10y z = -22, -2x + 3y + 10z = 22, using relaxation method. Taking $\Delta x = 0$, $\Delta y = 0$, $\Delta z = 0$.
- c. Find the largest Eigen value and the corresponding Eigen vector of the matrix,

$$A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$$
 by power method taking the initial Eigen vector as $\begin{bmatrix} 1, 1, 1 \end{bmatrix}^T$. 7

UNIT - V

9 a. Derive Euler's equation $\frac{\partial f}{\partial y} - \frac{d}{dx} \left(\frac{\partial f}{\partial y'} \right) = 0.$

b. Show that an extremal of
$$\int_{x_1}^{x_2} \left(\frac{y'}{y}\right)^2 dx$$
 is expressible in the form $y = ae^{bx}$. 7

c. Find the Geodesics on a surface given that the arc length on the surface is $S = \int_{x_1}^{x_2} \sqrt{x(1+y^{1^2})} dx$

10 a. Obtain the series solution of the equation $\frac{d^2y}{dx^2} + x^2y = 0$

b. Prove that
$$J_{\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \sin x$$
 and $J_{-\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \cos x$ 7

c. If
$$x^3 + 2x^2 - x + 1 = aP_0(x) + bP_1(x) + cP_2(x) + dP_3(x)$$
 Find the values of a, b, c, d. 7

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