



P.E.S. College of Engineering, Mandya - 571 401

(An Autonomous Institution affiliated to VTU, Belagavi)

Fourth Semester, B.E. - Electronics and Communication Engineering Semester End Examination; June - 2017 Digital Signal Processing

Time: 3 hrs Max. Marks: 100

Note: Answer FIVE full questions, selecting ONE full question from each unit.

UNIT - I

1 a. Find the *N*-Point DFT of the sequence $x(n) = 4 + \cos^2\left(\frac{2\pi n}{N}\right)$, $n = 0, 1, \dots, N-1$.

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b. State and prove frequency shifting property of DFT.

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c. Determine output of a FIR filter with impulse response

$$h(n) = 2\delta(n) + 2\delta(n-1) + \delta(n-2)$$

for an input x(n) given below. Using Overlap-add 8-point fast convolution technique.

$$x(n) = [3,0,-2,0,2,1,0,-2,-1,0]$$

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2 a. Find the 10-pint DFT of the sequences

$$(i) x(n) = \delta(n) + \delta(n-5)$$

$$(ii) x(n) = u(n) - u(n-6)$$

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- b. A signal $x_a(t)$ that is bandwidth to 10 kHz is sampled with a sampling frequency of 20 kHz. The DFT of N = 1000 samples x(n) is then computed.
 - (i) To what analog frequencies does the index k = 150 and 800 correspond to ?
 - (ii) Determine the spacing between spectral samples.

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c. If $x_1(n)$ and $x_2(n)$ are N-point sequences with N-point DFT's $x_1(k)$ and $x_2(k)$ respectively show that

$$\sum_{n=0}^{N-1} x_1(n) x_2^*(n) = \frac{1}{N} \sum_{n=0}^{N-1} x_1(k) x_2^*(k)$$

If
$$x_1(n) = x_2(n) = \cos\left(\frac{2\pi nk}{N}\right)$$
 determine $\sum_{n=0}^{N-1} x_1(n) x_2^*(n)$.

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UNIT - II

3 a. Compute 8-point DFT of the sequence x(n) = n+1 using decimation-in-freq FFT algorithm.

b. Use the 4-point inverse FFT to obtain the time-domain sequence given x(k) = [6, -2 + j2, -2, -2 - j2]

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c. Discuss the situation to justify use of chirp-Z transform.

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4 a. Develop the flowchart of decimation-in-freq FFT algorithm for a 8-point sequence starting from basic definition of DFT.

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b. Compute the DFT of the sequence x(n) = [1, 2, 3, 4, 4, 3, 2, 1] using 4-pont decimation in-time FFT algorithm only once.

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UNIT - III

5 a. Design a linear phase FIR high-pass filter using hamming window with a cutoff frequency $W_c = 0.8\pi \, \text{rad/sample}$ and N = 7. Given the desired frequency response as

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$$\begin{split} H_{d}(e^{jw}) &= e^{-jw\alpha}; \ -\pi \leq w \leq -w \quad \& \quad w_{c} \leq w \leq \pi \\ &= 0 \ ; \ otherwise \end{split}$$

- b. Discuss the steps used in design of FIR filler using frequency sampling method.
- c. Compare FIR & IIR filters for its various performance parameters.
- 6 a. Determine the coefficients of a linear-phase FIR-filter of length N=15, which has a symmetric unit sample response and frequency response that satisfies the condition

$$H\left(\frac{2\pi k}{15}\right) = 1; \text{ for } k = 0,1,2,3$$

$$= 0.4; \text{ for } k = 4$$

$$= 0; \text{ for } k = 5,6,7$$

- b. Discuss the effect of windows on the overall frequency response of FIR filter and list the ideal requirements of a window.
- c. Discuss the importance of linear phase in filters with examples.

UNIT - IV

7 a. An analog filter has a transfer function $H(s) = \frac{10}{s^2 + 7s + 10}$

Design a digital filter equivalent to this using impulse invariant method.

- b. Discuss the frequency axis mapping from analog to digital domain in impulse invariant method.
- c. Design a digital LPF using BLT to meet the following specifications.
 - (i) Monotonic pass band and stop band. (ii) -3dB cutoff at 0.5π rad/s.
 - (iii) -15dB attenuation at 0.75 π rad/s.
- 8 a. Derive the transformation function used with Bilinear transfer starting from basics and also comment on preservation of frequency selective characteristics in this transformation.
 - b. Design analog Butterworth filter that has a gain of -2 dB at 20 rad/s and attenuation in excess of 10dB beyond 30rad/sec

UNIT - V

- 9 a. Obtain a parallel realization of the transfer function $H(z) = \frac{10z^4 3.7z^3 1.28z^2 + 0.99z}{\left(z^2 + z + 0.34\right)\left(z^2 + 0.9z + 0.2\right)}$.
 - b. Discuss the ADPCM speech encoder which makes use of digital signal processor with a neat block diagram.
 - c. Realize Direct form-II structure for the system given by $H(z) = \frac{1 z^{-1}}{(1 + 0.5z^{-1} + z^{-2})}$.
- 10 a. An impulse response of a FIR filter is given by h(n) = [1, 2, 3, 4, 3, 2, 1], check whether the system has linear phase or not. If it has linear phase then obtain a realization using minimum numbers of multiplications.
 - b. Differentiate between speech analysis and synthesis. Discuss the various process involved in speech synthesis from text.
 - c. Realize the following transfer function in cascade form $H(z) = \frac{216z^3 + 96z^2 + 24z}{(2z+1)(12z^2 + 7z + 1)}$.