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## P.E.S. College of Engineering, Mandya - 571 401

(An Autonomous Institution affiliated to VTU, Belagavi)

**Fourth Semester, B.E. - Electronics and Communication Engineering**

**Semester End Examination; June - 2017**

**Electromagnetic Field Theory**

Time: 3 hrs

Max. Marks: 100

*Note: Answer FIVE full questions, selecting ONE full question from each unit.*

### UNIT - I

1. a. Derive an equation for electric field at a point due to finite length of line. 6
- b. A charge  $Q_A = -20 \mu\text{C}$  is located at A (-6, 4, 7), and a charge  $Q_B = 50 \mu\text{C}$  is at B (5, 8, -2) in free space. If distances are given in meters, find force on  $Q_B$  by  $Q_A$ . 4
- c. Calculate the total charge within each of the indicated volumes:
  - i)  $0.1 \leq |x|, |y|, |z| \leq 0.2; \rho_v = \frac{1}{(x^3 y^3 z^3)}$ ; 10
  - ii)  $0 \leq \rho \leq 0.1, 0 \leq \phi \leq \pi, 2 \leq z \leq 4; \rho_v = p^2 z^2 \sin 0.6\phi$
  - iii) universe:  $\rho_v = e^{-2r/r^2}$
2. a. State and explain Gauss's law and derive an equation in terms of the charge distribution. 8
- b. Point charge of  $0.25 \mu\text{C}$  is located at  $r = 0$ , and uniform surface charge densities are located as follows:  $2 \text{ mC/m}^2$  at  $r = 1 \text{ cm}$ , and  $-0.6 \text{ mC/m}^2$  at  $r = 1.8 \text{ cm}$ . Calculate  $\mathbf{D}$  at:
  - i)  $r = 0.5 \text{ cm}$                       ii)  $r = 1.5 \text{ cm}$                       iii)  $r = 2.5 \text{ cm}$ . 6
- c. State and explain the vector  $\nabla$  and the Gauss divergence theorem. 6

### UNIT - II

3. a. State and explain the followings along with the mathematical equations:
  - i) Potential difference                      ii) Absolute potential                      iii) Potential gradient. 6
- b. With the help of necessary equation show that  $\mathbf{E} = -\nabla V$  and explain the conservative nature of electric field. 8
- c. Define the current and current density along with their equations. 6
4. a. Current density is given in cylindrical coordinates as  $\mathbf{J} = -10^6 z^{1.5} \mathbf{A}_z \text{ A/m}^2$  in the region  $0 \leq \rho \leq 20 \mu\text{m}$ ; for  $\rho \geq 20 \mu\text{m}$ ,  $\mathbf{J} = 0$ .
  - i) Find the total current crossing the surface  $z = 0.1 \text{ m}$  in the  $az$  direction 8
  - ii) If the charge velocity is  $2 \times 10^6 \text{ m/s}$  at  $z = 0.1 \text{ m}$ , find  $\rho_v$  there
  - iii) If the volume charge density at  $z = 0.15 \text{ m}$  is  $-2000 \text{ C/m}^2$ , find the charge velocity there.
- b. Obtain the boundary conditions for perfect dielectric materials of permittivity's  $\epsilon_1$  and  $\epsilon_2$ . 7
- c. State and explain the uniqueness theorem. 5

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**UNIT - III**

- 5 a. Obtain an expression for the magnetic flux density at a point due to a current carrying straight conductor of finite length. Extend the analysis for the case of infinity long straight conductor. 10
- b. Evaluate the closed line integral of H about the rectangular path  $P_1(2, 3, 4)$  to  $P_2(4, 3, 4)$  to  $P_3(4, 3, 1)$  to  $P_4(2, 3, 1)$  to  $P_1$ , given  $H = 3za_x - 2x^3a_z$  A/m. 10
- i) Determine the quotient of the closed line integral and the area enclosed by the path as an approximation to  $(\nabla \times H)_y$       ii) Determine  $(\nabla \times H)_y$  at the center of the area.
6. a. Define the followings along with the mathematical equations: 9
- i) Force on a charged particle    ii) Force on a closed circuit    iii) Torque on a closed circuit.
- b. Explain the magnetization and permeability with the help of their equations. 6
- c. Discuss the concept of magnetic boundary conditions. 5

**UNIT - IV**

- 7 a. Explain the concept of displacement current. 6
- b. Briefly discuss the Maxwell's equations in integral forms. 7
- c. The electric field amplitude of a uniform plane wave propagating in the  $a_z$  direction is 250 V/m. If  $E = E_x a_x$  and  $\omega = 1.00$  Mrad/s, find: 7
- i) The frequency      ii) the wavelength      iii) the period      iv) The amplitude of H.
- 8 a. Write a short note on standing wave ratio. 5
- b. Explain the reflection of uniform plane waves at normal incidence. 8
- c. A uniform plane wave in air is normally incident on a dielectric slab of thickness  $\lambda/4$ , and intrinsic impedance  $\eta_2 = 260$ . Determine the magnitude and phase of the reflection coefficient. 7

**UNIT - V**

- 9 a. Explain the effects of imperfect earth and effects of curvature of earth. 8
- b. Explain the super refraction and scattering phenomena. 8
- c. Briefly explain the Tropospheric Propagation. 4
- 10 An Ionospheric wave is reflected from a layer of height of 200 km. The takeoff angle is  $20^\circ$  and the earth's radius is 6370 km. Calculate the skip distance if the earth is considered as: 6
- i) flat surface    ii) spherical.
- b. Calculate the skip distance for flat earth with MUF of 10 MHz if the wave is reflected from a height of 300 km where the maximum value of n is 0.9. 8
- c. Explain the term critical frequency, MUF, LUF. 6