

Time: 3 hrs

Max. Marks: 100

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Note: Answer FIVE full questions, selecting ONE full question from each unit.

UNIT - I

1 a. Determine the 4-point DFT of sequence given by,

 $x(n) = \frac{1}{3}; \qquad 0 \le n \le 2$ = 0; otherwise Draw its magnitude and phase spectra

b. Consider a length-12 sequence defined for

$$0 \le n \le 11$$

 $x(n) = \{8, 4, 7, -1, 2, 0, -2, -4, -5, 1, 4, 3\}$
with 12 point DFT $x(k); 0 \le n \le 11$
Evaluate the DFT

$$\sum_{k=0}^{11} e^{-j\frac{4\pi k}{6}} x(k)$$

- c. Given that X(k) and Y(k) are the 6-point DFT of sequence x(n) and y(n) respectively x(k) = {1+j, -2.1+j3.2, -1.2-j2.4, 0, 0.9+j.31, -0.3+j1.1} The sequence x(n) and y(n) are related by y(n) = x((n-4))₆ Determine Y(k) without computing the DFT.
- 2 a. Obtain the 4-point DFT of the sequence $x_1(n) = \{1, 1, 2, 3\}$ and thereby find the 4-point DFT of the sequence $x_2(n) = \{1, 3, 2, 1\}$ using the appropriate property.
 - b. Compute the eight point circular convolution of the following sequences :

$$\mathbf{x}(\mathbf{n}) = \mathbf{u}(\mathbf{n}) \mathbf{-} \mathbf{u}(\mathbf{n} \mathbf{-} \mathbf{4})$$

and h(n) = u(n)-u(n-3)

c. Find the output y(n) of a filter whose impure response is $h(n) = \{1, 1, 1\}$ and input signal is $x(n) = \{3, -1, 0, 1, 3, 2, 0, 1, 2, 1\}$ using overlap save method, assuming the length of block as 5.

UNIT - II

3 a. Determine the 8-point DFT the sequence x (n) =2ⁿ ; 0 ≤ n ≤ 7 use DIT-FFT algorithm.
b. Compute the four point DFT of the sequence x(n) = {1, 2, 1, 2} using the Goertzed algorithm.
c. Obtain the 4 point IDFT of the sequence X(k) = {10, -2+j2, -2, -2-2j}using DIT-FFT algorithm.
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4 a. Determine the DFT of Hamming window $w(n) = 0.54 - 0.46 \cos(2\pi n / (N-1), 0 \le n \le 7)$ using the signal flow graph of DIF-FFT.

- b. A 512 point DFT of a sequence of length 498 is to be computed.
 - i) How many Zero valued samples should be appended to x (n) prior to the computation of the DFT radius-2 DIT-FFT algorithms?
 - ii) What are the total number of complex multiplications and additions needed for the direct6 evolution of all DFT samples?
 - iii) What are the total number of complex multiplications and addition needed if a radix-2 DIT-FIT algorithm is used?
- c. Determine the time domain representation of

 $X(k) = \{7, 1, -j2, -1, 1+j2\}$ using DIF = FFT algorithm.

UNIT - III

- 5a. Design a low-pass FIR filter using rectangular window with cut-off frequency $W_c = \pi/2$ radian. The length of the impulse response should be 11. Also obtain the expression to find the 12 magnitude response.
- b. If the frequency response of a liner phase FIR filter is given by H (e^{iw}) = [0.3+0.5 cos(w)+0.3cos(2w)]. Determine the filter coefficients.
- c. List the advantages and disadvantages of a FIR filter.
- 6a. Design a FIR high pass filter with frequency response

$$H_{d}(e^{jw}) = \begin{cases} e^{-jwT}; & W_{c} \le |w| \le \pi \\ 0 & ; & 0 \le |w| \le Wc \end{cases}$$
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Find the value of h(n) for N = 7 using Hamming window.

b. Design a linear phase FIR filter wire N = 7 are cut-off frequency of $W_c = 0.3 \pi$ rad using the frequency sampling method.

UNIT - IV

- 7a. Design a digital Butterworth low pass filter with frequency specification given by,
 - i) Passband \leq 3.01 dB ii) Passband edge frequency : 500 Hz 12
 - iii) Stop band attenuation ≥ 15 dB iv) Stop band edge frequency :750 Hz

v) Sampling rate $f_s = 2$ kHz use bilinear transformation method.

b. Using bilinear transformation, convert the low pass filter given by,

$$H_{Lp}(s) = \frac{1}{S^2 + \sqrt{2} S + 1}$$

In to a digital high pass filter with pass band edge $f_p = 100$ Hz and Sampling frequency 1 kHz

8 a. Design a Chebyshev-I low pass filter with ripple of 1 dB in the password $0 \le w \le 0.2\pi$ and attenuation of atleast 15 dB in the stop band $0.3 \le w \le \pi$. Use impulse invariant method.

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b. Given an analog filter with transfer function

$$Ha(s) = \frac{(s+2)}{(S+1)(S+3)}$$

Find the corresponding digital IIR filter H(z) using matched Z-transfer method. Given that Sampling rate is 10Hz.

UNIT - V

- 9 a. Obtain direct form I, direct from-II, cascade and parallel form realization for the following system Y (n) = 0.75y(n-1) - 0.125y(n-2) + 6x(n) + 7x(n-1) + x(n-2).14
 - b. Realize a linear phase filter given by

$$h(n) = \left(\frac{1}{2}\right)^n [u(n) - u(n-4)] \text{ using direct form-I.}$$

10 a. Obtain block diagram of the direct form I and direct form II realization for a digital IIR filter described by the system function

$$H(z) = \frac{8Z^{3} - 4Z^{2} + 11Z - 2}{\left(Z - \frac{1}{4}\right)\left(Z^{2} - Z + \frac{1}{2}\right)}$$
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- b. Explain the ADPCM speech encoding process
- c. Find the transfer function and difference equation representation for the system in Fig Q.10

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