



**P.E.S. College of Engineering, Mandya - 571 401**

(An Autonomous Institution affiliated to VTU, Belagavi)

Fourth, Semester, B.E. - Electrical and Electronics Engineering

Semester End Examination; May/June - 2018

Signals and Systems

Time: 3 hrs

Max. Marks: 100

Note: Answer **FIVE** full questions, selecting **ONE** full question from each unit.

**UNIT - I**

- 1 a. i) Evaluate the integral  $\int_{-\infty}^{\infty} (t-1)\delta(\frac{2}{3}t - \frac{3}{2}) dt$       ii) Sketch the signal  $x(t) = \delta(\cos t)$  5
- b. Determine whether the signal  $x[n] = (-1)^n$  is periodic and find fundamental period. 5
- c. Express  $x_2(t)$  in terms of  $x_1(t)$  in Fig.1(c).

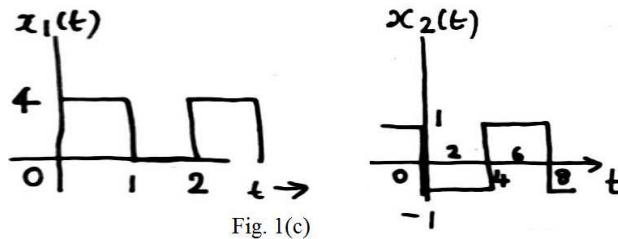


Fig. 1(c)

- d. For the signal  $x(t)$  of Fig. 1(d) plot  $2x(2t+2)$ .

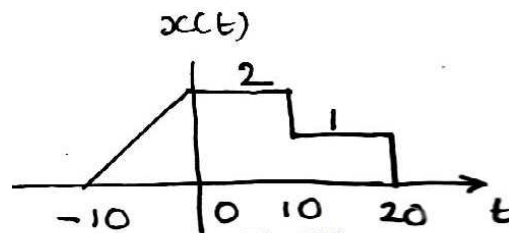


Fig. 1(d)

- 2 a. Determine whether the system described by  $y[n] = \cos(x[n+2])$  is,
- i) Memory-less      ii) Invertible      iii) Causal 10
- iv) Stable      v) Time invariant      vi) Linear

- b. Consider the signal

$$x(t) = \cos 5t + 3e^{-j10t},$$

Find fundamental period  $T_o$  and angular frequency  $w_o$ .

- c. Let  $x(t)$  and  $y(t)$  be given in Fig. 2(c), sketch  $x(t) y(t-1)$ .

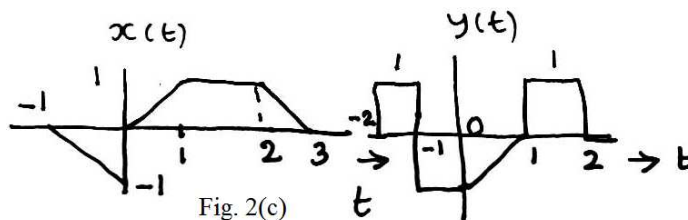


Fig. 2(c)

UNIT - II

3 a. Consider the continuous time signals depicted in Fig. 3(a). Evaluate the convolution integral  $y(t) = x(t) \times h(t)$ .

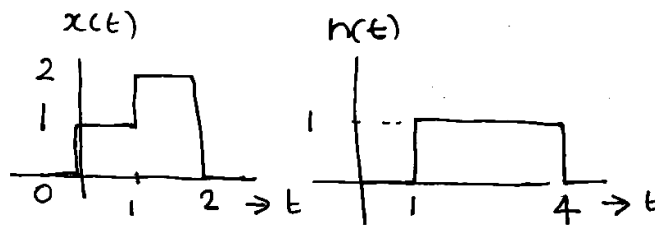


Fig. 3(a)

15

b. State the properties of convolution.

5

4 a. Given  $x[n] = \{0, 1, 2, 3, 4, 5, 0, \dots\}$

$h[n] = \{0, 1, 2, 3, 4, 5, 0, \dots\}$

10

Evaluate  $x[n] \times h[n]$  at  $n = 0, 2$ .

b. The impulse response of the discrete LTI system is

$$h[n] = n \left(\frac{1}{2}\right)^n u[n]$$

10

Check the following :

- i) Stability
- ii) Causality

UNIT - III

5a. Determine the forced response for the system described by the following difference equation;

$$y[n] - \frac{2}{5} y[n-1] = 2x[n] \text{ where input } x[n] = -\left(\frac{1}{2}\right)^n u[n]$$

5

b. Draw direct form-I and form-II implementation for the difference equation;

$$y[n] + \frac{1}{4} y[n-1] - \frac{1}{4} y[n-2] = x[n] + x[n-1]$$

10

c. Find difference equation description for the system depicted in Fig. 5(c).

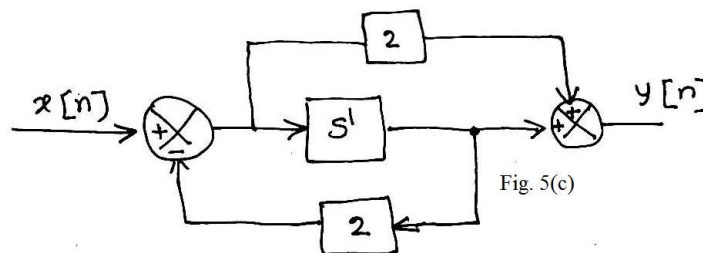


Fig. 5(c)

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6 a. For the periodic waveform shown in Fig. 6(a) find the exponential Fourier series and sketch magnitude and phase spectra.

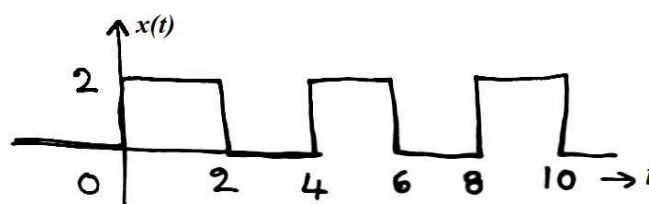


Fig. 6(a)

10

- b. Use the definition of the Fourier series to determine the time signal represented by the following Fourier series coefficients 10
- $$X[k] = j\delta[k-1] - j\delta[k+1] + \delta[k-3] + \delta[k+3] \quad \omega_0 = 3\pi \text{ rad/sec.}$$

**UNIT - IV**

- 7 a. Use the defining equation for the Fourier transform to evaluate the frequency domain representations for the signal, 10
- $$x(t) = e^{-|t|} \text{ Sketch magnitude and phase spectra.}$$

- b. Find the Fourier transform  $X(\omega)$ . Given  $x(t) = \cos(\omega_0 t) u(t)$ . 10

- 8 a. Find the Fourier transform  $X(\omega)$  of the signal 10
- $$x(t) = \frac{1}{1+jt}$$

- b. State: i) Periodicity ii) Linearity iii) Time shift 10  
 iv) Time reversal v) Frequency shift properties of DTFT

**UNIT - V**

- 9 a. Determine the Z-transform of;
- $$x[n] = \left(\frac{1}{2}\right)^n u[n] + 2^n u[n] \quad \text{10}$$

and depict the ROC and the location of poles and Zeros in the Z-plane.

- b. i) State and prove initial value theorem  
 ii) Find the initial value  $x[n]$  given 10
- $$X[z] = \left( \frac{1 - z^{-1} + z^{-2}}{(1 - (1/2)z^{-1})(1 - 2z^{-1})(1 - z^{-1})} \right)$$
- with ROC  $1 < |z| < 2$

- 10 a. Find the inverse Z-transform of 6
- $$X[z] = \frac{1 + z^{-1}}{1 - (1/3)z^{-1}}$$
- when ROC :  $|z| > \frac{1}{3}$  using longdivision method.

- b. Find the inverse Z-transform of 14
- $$X(z) = \frac{1 - z^{-1} + z^{-2}}{(1 - (1/2)z^{-1})(1 - 2z^{-1})(1 - z^{-1})}$$
- with ROC  $1 < |z| < 2$

Using partial fraction expansion.