



**P.E.S. College of Engineering, Mandya - 571 401**

*(An Autonomous Institution affiliated to VTU, Belagavi)*

**Second Semester, M. Tech - Civil Engineering (MCAD)**

**Semester End Examination; May/June - 2018**

**Reliability Analysis and Design of Structural Elements**

*Time: 3 hrs*

*Max. Marks: 100*

- Note: i) Answer FIVE full questions, selecting ONE full question from each unit.  
ii) Use of CDF table for Normal distribution is permitted.*

**UNIT - I**

- 1 a. Find the missing frequency for the frequency distribution. Given Mean = 33.5, Mode = 34,  $\Sigma f_i = N = 230$ .

CI	0-10	10-20	20-30	30-40	40-50	50-60	60-70
$f_i$	4	16	-	-	-	6	4

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- b. The following are the test results obtained on an experiment.

2	7	9	10	20	21	22	13	14	13	19	26	28	15	16
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Calculate the mean, standard deviation and coefficient of variation. Plot a histogram.

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Determine the chance of getting a value

- (i) less than 6      (ii) between 12 & 18      (iii) greater than 24

- 2 a. Define the first four central moments about mean, show that the first central moment is equal to zero.

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- b. Write a short note on skewness and Kurtosis.

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- c. The cube strengths of concrete follow the normal distribution with mean of 42.28 N/mm<sup>2</sup> and standard deviation of 5.6 N/mm<sup>2</sup>. Calculate the probability of getting a value for a strength less than 35 N/mm<sup>2</sup>

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- d. The compressive strength of steel follows the 10g normal distribution with mean of 460 N/mm<sup>2</sup> and having a coefficient of variation of 20%. Determine the probability of the yield strength being less than 415 N/mm<sup>2</sup>

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**UNIT - II**

- 3 a. List the properties of correlation coefficient.

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- b. Fit an exponential curve of the form  $y = abx$  to the following data. Estimate the population in the year 2006.

Year ( $x_i$ )	1931	1341	1951	1961	1971	1981	1991
Population (y) in lakhs	3.9	5.3	7.3	9.6	12.9	17.1	23.2

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- 4 a. Calculate the correlation co-efficient between X and Y for the following data. What do you infer?

x	5	15	18	20	25	25	30	34	38	50
y	45	32	37	33	24	29	26	22	24	15

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- b. Fit a straight line of the form  $y = a+bx$  to the following data:

x	71	68	73	69	67	65	66	67
y	69	72	70	90	68	67	68	64

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**UNIT - III**

- 5 a. A tension member of a steel truss is subjected to an axial load Q. The strength of the member is given by  $f_y.A$ . Where  $f_y$  is the yield strength of steel and A is the area of cross section of the member.

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Given:  $Q = N(20, 8)$  KN,  $f_y = N(286, 28.6)$  N/mm<sup>2</sup>. Find the area of the member for the specified reliability of 0.99865 considering 3% variation in area.

- b. A simply supported beam of span 'l' is subjected to a uniform distributed load of 'w' KN/m throughout the span. Establish the statistics of maximum deflection

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Given:  $l = N(4.3, 0.35)$ m,  $w = N(32, 2.6)$ KN/m

$E = N(2 \times 10^5, 0.2 \times 10^5)$ N/mm<sup>2</sup>,  $I = N(4.5 \times 10^7, 230 \times 10^6)$ mm<sup>4</sup>

- 6 a. It is assumed that the strength of a RCC column is given by the sum of the strengths of concrete ( $f_{ck}$ ) & reinforcing bars ( $f_y$ )

Given  $f_{ck} = N(25, 5)$  N/mm<sup>2</sup>,  $f_y = N(460, 46)$  N/mm<sup>2</sup>

If the size of the column is 250mm x 400mm and it is provided with 4 bars of 20 mm diameter bars. Determine the mean value of standard deviation of the strength of the column. The column is subjected to a Dead load & live load with distribution N (1500,200) kN and N(500,200) kN respectively. Compute the reliability of the column.

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- b. A cantilever beam of span 'l' is subjected to a uniformly distributed load of 10 kN/m throughout the span. Establish the statistics of maximum Bending moment. (Given:

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$l = N(4, 0.35)$ m,  $w = N(25, 2.5)$  kN/m

**UNIT - IV**

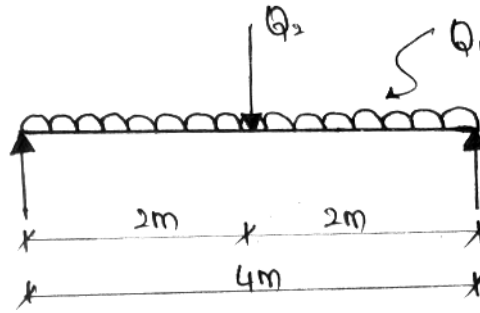
7. Calculate the reliability index and probability of failure by FDSM method, of the beam against the limit state of collapse in flexure shown in figure subjected to a self weight of  $Q_1$  and a live load  $Q_2$ . The flexural resisting moment capacity of the beam is R. It is given that :

$Q_1 = N(400, 10)$  N

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$Q_2 = N(5000, 2000)$  N

$R = N(10,000, 1000)$  N.m



8. Determine the reliability index by FOSM method for a steel tension member having tensile strength  $R$ , subjected to a tensile load  $Q$ .

Given  $R = N(280,28) \text{ N/mm}^2$

$Q = N(5000,2000) \text{ N}$

$D = N(6,0.6) \text{ mm}$

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The member is circular in cross section of diameter  $D$ . The safety margin is given by (i)

$$M = \frac{\pi D^2}{4} - \frac{Q}{R} \quad \text{(ii) } M = D - 2\sqrt{\frac{Q}{\pi R}}$$

**UNIT - V**

9. Determine the reliability index by AFOSM (Hasofer-lind) method for a steel tension member having tensile strength  $R$ , subjected to a tensile load  $Q$ .

Given  $R = N(280, 28) \text{ N/mm}^2$

$Q = N(5000,2000) \text{ N}$

$D = N(6,0. 6) \text{ mm}$

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The member is circular in cross section of diameter  $D$ . failure function is given by (i)

$$R = \frac{4Q}{\pi D^2} - 0$$

10. The strength  $R$  of an axially located column is given by  $R = 83750C + 1250F$

Where  $C$  is the compressive strength of concrete.  $F$  is the yield strength of steel. The variable  $C$  &  $F$  are normally distributed with parameters  $N(19.54, 4.1) \text{ N/mm}^2$  and  $N(469, 46.9) \text{ N/mm}^2$  respectively. Determine the statistics of  $R$  using Monte Carlo method ( 10 values) Compare the values with the theoretical value and find the percentage error.

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