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## P.E.S. College of Engineering, Mandya - 571401

(An Autonomous Institution affiliated to VTU, Belagavi)
Second Semester, M.Tech. - Mechanical Engineering (MMDN)
Semester End Examination; May / June - 2019
Dynamics and Mechanism Design
Time: 3 hrs
Max. Marks: 100
Note: i) Answer FIVE full questions, selecting ONE full question from each unit.
ii) Missing data, if any, may be suitably assumed.

## UNIT - I

1 a. Explain Holonomic and Non-Holonomic constraints with example.
b. Write a note on :
i) Coordinate transformation
ii) Generalized force
iii) Generalized momentum

2 a. Two frictionless blocks of equal mass $m$ are connected by a mass less rigid rod as shown in Fig. Q2(a). Obtain the force $\mathrm{F}_{2}$ if the system is in static equilibrium.


Fig. Q 2(a)
b. Prove that the work done on a particle depends upon its initial and final position.
c. A ball of mass $m$ is sliding along a rigid rod as shown in Fig. Q2(c). If the position of mass is given by the spherical coordinates $(r, \theta, \phi)$, obtain the expression for the kinetic energy and the generalized momenta.


Fig. Q 2(c)
UNIT - II
3 a. A simple pendulum of length $L$ and weight $m g$ is pivoted to the mass $M$ which slides without friction on a horizontal plane as shown in Fig. Q3(a). Use LaGrange's equation to determine the equations of motion of the system and hence approximate the equations for small oscillations.


Fig. Q 3(a)
b. A particle of mass $m$ can slide without friction on the inside of a small tube which is bent in the form of a circle of radius $r$. The tube rotates about a vertical diameter with a constant angular velocity as shown in Fig. Q3(b). Obtain the differential equation of motion.


Fig. Q3(b)
4 a. Derive Hamilton's equation from LaGrange's equation.
b. Derive Euler's equation of motion.

## UNIT - III

5 a . The characterstics of eqation of a system is given by, $\mathrm{s}^{4}+12 \mathrm{~s}^{3}+10 \mathrm{~s}^{2}+2 \mathrm{~s}+K=0$.
Determine the value of $K$ for the system to be stable.
b. Explain the following controller:
i) Proportional controller
ii) Proportional plus derivative controller

6 a. State Grashof's law and specify the conditions with necessary sketches, for obtaining different kinematic inversion of a quadratic chain.
b. Determine the mobility of mechanisms shown in Fig. Q6(b) using Kutzbzch criterion.


Fig. Q 6(b)
c. For the mechanism shown in Fig. Q6(c), draw equivalent kinematic chain with turning pairs.

(i)

(ii)

## UNIT - IV

7 a. A crank-rocker mechanism is having a time ratio of one, output rocker angle of $60^{\circ}$ and minimum transmission angle of $40^{\circ}$. If the length of fixed link is 50 mm , design the mechanism for its maximum transmission angle.
b. Using relative pole method synthesize a slider crank mechanism with eccentricity $e=15 \mathrm{~mm}$ for the two positions of input link $\theta_{12}=30^{\circ}$ and output displacement $S_{12}=45 \mathrm{~mm}$ of slider. The slider should move away from the fixed center while input crank moves in clockwise direction.

8 a. Explain Bloch's method for the synthesis of four-link mechanism.
b. Using Freudenstein's equations, synthesis a 4-link mechanism to coordinate three positions of the input and output links as follows:
$\theta_{1}=20^{\circ}, \theta_{2}=35^{\circ}, \theta_{3}=50^{\circ}$ and $\phi_{1}=35^{\circ}, \phi_{2}=45^{\circ}, \phi_{3}=60^{\circ}$.
UNIT - V
9 a. Synthesis a four-link mechanism to coordinate three positions of the input and output links for the following angular displacement by inversion method :
$\theta_{12}=35^{\circ}, \theta_{13}=80^{\circ}$, and $\phi_{12}=50^{\circ}, \phi_{13}=80^{\circ}$.
Input and output links rotate counter clock wise direction
b. Using point position reduction technique, design a four-link mechanism so that the input and output links have the following angular position :
$\theta_{12}=20^{\circ}, \theta_{23}=30^{\circ}, \theta_{34}=40^{\circ}$ and $\phi_{12}=40^{\circ}, \phi_{23}=30^{\circ}, \phi_{34}=20^{\circ}$.
10. Write a short notes on :
a) Overlay method
b) Coupler curve synthesis
c) Congnate linkages
d) Caley's diagram

