P.E.S. College of Engineering, Mandya - 571 401 (An Autonomous Institution affiliated to VTU, Belagavi) Third Semester, B.E. - Semester End Examination; Dec. - 2019 Transform Calculus Fourier series and Numerical Techniques

U.S.N

(Common to all Branches)

Max. Marks: 100

Time: 3 hrs

Course Outcomes

The Students will be able to:

CO1: Apply the knowledge of calculus to solve problems related to polar curves and its applications in determining the bentness of a curve.

CO2: Explain mean value theorems and evaluate the indeterminate form and power series using Taylors and Maclaurin's series.

CO3: Differentiate the function of several variables differentiate the composite function. Evaluate the vector differentiation.

CO4: Evaluate some standard integrals by applying reduction formula and solve application problems. Solve differential equations of first order and solve application problems in engineering field.

Note: I) PART - A is compulsory, one question from each unit.

II) PART - B: Answer Two sub-questions for Maximum of 18 marks from each unit.

| Q. No. | Questions | | | | | | | | BLs | COs |
|--------|--|---------|---------|---------|---------|---------|--------|---|-----|-----|
| | I : PART - A | | | | | | | | | |
| I a. | Write Newton's backward interpolation formula upto fourth degree term. | | | | | | | | L1 | CO1 |
| b. | Write Sterling's formula upto third terms. | | | | | | | | L1 | CO1 |
| с. | Evaluate $\int (x+x^2) \cos nx dx$. | | | | | | | | L1 | CO3 |
| d. | Define Infinite Fourier Transform and inverse Fourier Transform. | | | | | | | | L1 | CO4 |
| e. | Solve: $\frac{\partial^2 z}{\partial x \partial t} = e^{-t} \cos x$ | | | | | | | | L1 | CO4 |
| | II : PART - B | | | | | | | | | |
| | UNIT - I | | | | | | | | | |
| 1 a. | From the following table find the number of students who obtained between 40 and 45 marks. | | | | | | | | L2 | CO1 |
| | Marks | 30 - 40 | 40 - 50 | 50 - 60 | 60 - 70 | 70 - 80 | | 9 | L2 | COI |
| | No. of students | 31 | 42 | 51 | 35 | 31 | | | | |
| b. | Construct the interpolation polynomial for the data given below using Newton's divided difference formula. | | | | | | | | | |
| | x 2 | 2 | 4 | 5 | 6 | 8 | 10 | 9 | L2 | CO1 |
| | y 1 | 0 | 96 | 196 | 350 | 868 | 1746 | | | |
| | Hence find the value of <i>y</i> when $x = 7$ and $x = 9$ | | | | | | | | | |
| | | | | | | | Contd2 | | | |

| 1 8M / | | | | | | • | | 1 . | | Pu | ge No | о 2 |
|---------------|---|--------------------------------|-------------------|-----------------------|-------------------------|--|-----------------|---|---------------|----|-------|-----|
| | i) Write Gauss's backward interpolation formula up to third degree terms.ii) Using Stirling's formulae, estimate the value of tan (16°) and from the data. | | | | | | | | | | | |
| | | 0 | 5 | 10 | | 2 | | 25 | 30 | 9 | L3 | CO |
| | $\frac{x}{\operatorname{Tan}(x)}$ | 0 | 0.0875 | 0.1763 | 0.267 | | | 0.4663 | 0.5774 | | | |
| | $\operatorname{Tan}(\lambda)$ | U | 0.0075 | | JNIT – I | | 557 | 0.4005 | 0.5774 | 18 | | |
| 2 a. | i) Write fir | st deriv | vative of | Newton's | backwa | d formu | la up to | 3 rd deg | ree term. | | | |
| | i) Write first derivative of Newton's backward formula up to 3rd degree term. ii) Find the maximum and minimum value of y from the data. | | | | | | | | | | | - |
| | [| x: | -2 | -1 0 | | 2 | 3 | 4 | 7 | 9 | L3 | CO |
| | - | y: | | -0.25 0 | - | | 15.75 | | | | | |
| b. | i) Write Sin | mpson' | | | | 1 1 | | | | | | |
| | ii) The velo | ocity 'י | v' of a p | article at o | distance ' | s' from | a point | on its p | ath is give | en | | |
| | by the table | 2: | | | | | | | | | | |
| | | X(ft | t) 0 | 10 | 20 3 | 0 40 | 50 | 60 |] | 9 | L2 | CO |
| | | V(fts | | 58 | 64 6 | 5 61 | 52 | 38 | | | | |
| | | Ť | | | | | | | | | | |
| | Estimate th | le time | taken to | travel 60 | ft by usii | ng Simps | son's 1/ | 3 rd rule. | | | | |
| c. | Evaluate: | $\frac{1}{1}$ | dx using | Boole's 1 | ule for <i>n</i> | = 4 and | Weddle | e's rule f | for $n = 6$. | 9 | L2 | CO |
| | Evaluate: $\int_{0}^{1} \frac{1}{1+x^{2}} dx$ using Boole's rule for $n = 4$ and Weddle's rule for $n = 6$. | | | | | | | | | | | |
| | UNIT - III | | | | | | | | | 18 | | |
| 3 a. | Expand the | e Four | ier serie | s of $f(x)$ | $)=\pi^2-x$ | r^2 in $-\pi$ | $x \le x \le x$ | au and he | nce dedu | ce | | |
| | that, | | | | | | | | | | | |
| | i) $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots - \infty = \frac{\pi^2}{12}$ | | | | | | | | | 0 | 1.0 | |
| | | | | | | | | | | 9 | L2 | CO. |
| | ii) $\frac{1}{1^2} + \frac{1}{2^2}$ | 1 | 1 | | π^2 | | | | | | | |
| | ii) $\frac{1}{1^2} + \frac{1}{2^2}$ | $+\frac{1}{3^2}+\frac{1}{3^2}$ | $\frac{1}{4^2} +$ | | $-\infty = \frac{1}{6}$ | - | | | | | | |
| | | | | | | ſ | | l | | | | |
| b. | Obtain half | range | sine and | cosine se | ries of | $f(x) = \begin{cases} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$ | <i>kx</i> ,0 | $\leq x \leq \frac{1}{2}$ | | 9 | L3 | CO |
| | | Tunge | Sine une | | 1105 OF J | | k(1-x) | $\left(\right), \frac{l}{2} \leq x \leq x$ | $\leq l$ | | 13 | 0.0 |
| | | | | | | ί | | 2 | | | | |
| c. | The follow | ing dat | ta gives t | he variation | ons of a p | periodic o | current | over a p | eriod. | | | |
| | t sec: | 0 | | | | | 2T/3 | 5T/6 | Т | | | ~~ |
| | <i>i</i> amp | 1.9 | | | | | -0.88 | -0.25 | | 9 | L2 | CO. |
| | Show that | there i | | | - | - | | variable | current ar | nd | | |
| | | - | | and the second second | nd second | | 100 | | | | | |
| | obtain the | e ampl | itude of | the first ar | iu secone | I narmon | 105. | | | | | |
| | | e ampl | itude of | the first ar | | i narmon | 105. | | Contd3 | | | |

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| | UNIT - IV | 18 | | |
|------|--|----|----|-----|
| 4 a. | If $f(x) = \begin{cases} 1 - x^2, x < 1 \\ 0, x \ge 1 \end{cases}$ Find the Fourier transform of f(x) and hence find the value of $\int_{0}^{1} \frac{x \cos x - \sin x}{x^3} dx$ | 9 | L2 | CO4 |
| b. | i) Obtain the Fourier sine transform of the functions, $f(x) = \begin{cases} 4x, & 0 < x < 1\\ 4-x, & 1 < x < 4\\ 0, & x > 4 \end{cases}$ ii) Find the Fourier cosine transform of $e^{- x }$ | 9 | L2 | CO4 |
| c. | i) State initial value and final value theorems for Z-transform. ii) Solve difference equation $u_{n+2} + 4u_{n+1} + 3u_n = 3^n$ with $u_0 = 0, u_1 = 1$. | 9 | L3 | CO4 |
| | UNIT - V | 18 | | |
| 5 a. | i) Form the PDE by eliminating arbitrary constant in $z = a \log (x^2 + y^2) + b$ ii) Form the PDE by eliminating arbitrary functions $z = y^2 + 2f (1/x + \log y)$ | 9 | L1 | CO4 |
| b. | i) Define linear PDE. ii) Solve $(z^2 - 2yz - y^2) p + (xy + xz) q = xy - xz$ | 9 | L2 | CO4 |
| c. | Find the various possible solutions of the two dimensional Laplace's equation by the method of separation of variables. | 9 | L2 | CO4 |

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