



## P.E.S. College of Engineering, Mandya - 571 401

(An Autonomous Institution affiliated to VTU, Belagavi)

**First Semester, Master of Computer Applications (MCA)**

**Semester End Examination; Jan. - 2020**

**Discrete Mathematical Structures**

Time: 3 hrs

Max. Marks: 100

*Note: Answer FIVE full questions, selecting ONE full question from each unit.*

### UNIT - I

- 1 a. How many numbers greater than 1000000 can be formed by using the digits 1, 2, 2, 2, 4, 4, 0? 6
- b. Find the number of permutations of the letter of the following words, 7
  - i) PROGRESS            ii) TOPOLOGY            iii) ENGINEERING
- c. Find the coefficient of the following,
  - i)  $x^3 y^3 z^3 w^1$  in the expansion of  $\left(2x + \frac{y}{3} - z + w\right)^{10}$  7
  - ii)  $a^5 b^{10} c^{15}$  in the expansion of  $\left(\frac{a}{2} + 4b + 3c + d\right)^{30}$
- 2 a. For any three sets A, B, C prove that  $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$  6
- b. In a sample of 100 logic chips. 23 have a defect  $D_1$ , 26 have a defect  $D_2$ , 30 have defect  $D_3$ , 7 have defects  $D_1$  and  $D_2$ , 8 have defective  $D_1$  and  $D_3$ , 10 have defectives  $D_2$  and  $D_3$  and 3 have all three defectives. Find the number of chips having, (i) at least one defective (ii) no defect. 7
- c. A fair die is tossed twice. Find the probability that,
  - (i) Even numbers occur on both throws 7
  - (ii) An even number occurs at least one throw.

### UNIT - II

- 3 a. Verify that:  $[p \rightarrow (q \rightarrow r)] \rightarrow [(p \rightarrow q) \rightarrow (p \rightarrow r)]$  is tautology. 6
- b. Prove:  $\neg[\{(p \vee q) \wedge r\} \rightarrow \neg q] \Leftrightarrow q \wedge r$  is logical equivalence by using laws. 7
- c. Express symbolically and check validity of the given argument
 

Ram will get driving license or  
He will join as a job driver 7  
If Ram do not get loan, Ram will join as a job driver  
Ram got DL, Therefore Ram will not join as a job driver.
- 4 a. Define quantifiers with an example. 4
- b. Define rule of universal specification and generalization. 4
- c. Write down the following proposition in symbolic form and find its negation "For all integers  $n$ , if  $n$  is not divisible by 2 then  $n$  is odd" 6

d. Prove that the following argument is valid

$$\begin{array}{l} \forall x [p(x) \rightarrow q(x)] \\ \forall x [q(x) \rightarrow r(x)] \\ \hline \neg r(c) \\ \hline \therefore \neg p(c) \end{array}$$

6

**UNIT - III**

5 a. If  $n$  is a positive integer then prove that  $1.2 + 2.3 + 3.4 + \dots + n(n + 1) = \frac{n(n+1)(n+2)}{3}$  6

b. Define One–One function, Onto function and find the number of One-One and Onto functions from a set of  $m$  elements to a set of  $n$  elements. 7

c. Write the recursively relation for,  
i)  $a_n - 4n + 1 \quad a_0 = 1, n \geq 1$  7

ii)  $a_n = 5a_{n-1}, n \geq 1, a_0 = 2.$

6 a. Show that if seven numbers are selected 1 to 12, then two of them will add upto 13. 6

b. State pigeon hole principle. Find the least number of ways of choosing three different numbers from 1 to 10 so that all choices have the same sum. 7

c. Define permutation function, Hashing function and characteristic function. 7

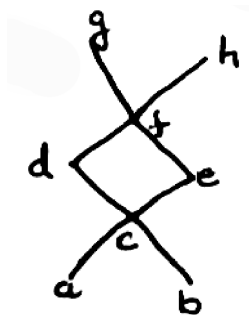
**UNIT - IV**

7 a. Let  $A = \{1, 2, 3, 4, 6\}$  and  $R$  be a relation on  $A$  defined by  $a R b$  iff  $a$  is a multiple of  $b$  represent  $R$  as a set of ordered pairs. Draw the diagraph and matrix representation of  $R$ . 6

b. Define partially ordered set and draw the Hasse diagram of all positive divisors of 36. 7

c. Prove that the Relation  $R = \{(1, 1) (1, 2) (2, 1) (2, 2) (3, 4) (4, 3) (3, 3) (4, 4)\}$  is an equivalence relation defined on the set  $A = \{1, 2, 3, 4\}$ . Also determine the partition induced. 7

8 a. Consider the Hasse diagram of a poset  $(A, R)$  given below,

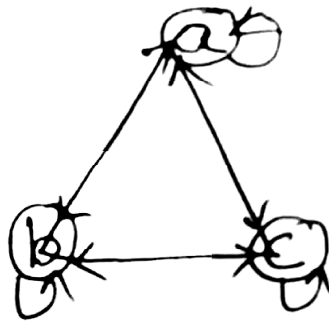


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If  $B = \{c, d, e\}$  find,

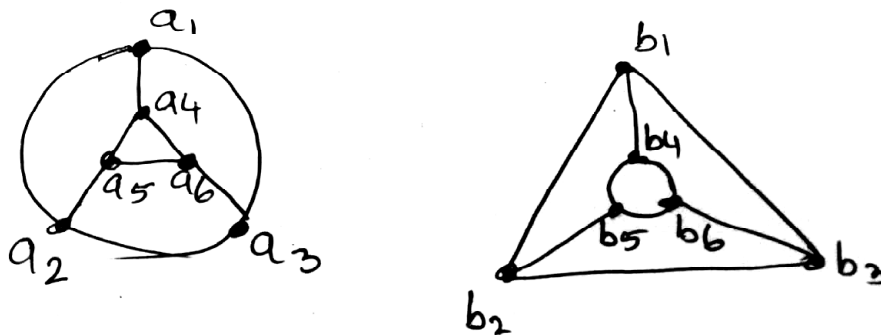
- i) All upper bounds of  $B$
- ii) All lower bounds of  $B$
- iii) The *LUB* of  $B$
- iv) The *GLB* of  $B$

- b. Draw four graphs that represent a lattice with valid reason. 7
- c. A relation  $R$  on the set  $\{a, b, c\}$  is represented by the diagram below. Write  $R$  and prove that  $R$  is an equivalence relation. 7



UNIT - V

- 9 a. Show that the graphs are isomorphic, 6



- b. Write short note on Konigsberg bridge problem related to origin of graph theory. 7
- c. Prove that “A graph with  $n$  vertices is a tree if it is connected, posses  $(n-1)$  edges and conversely”. 7
- 10 a. Define Rooted tree, M-ary tree and Balanced tree with an example for each. 6
- b. Construct an optimal prefix code for the letters of the word ENGINEERING. Hence deduce the code for this word. 7
- c. Define minimal spanning tree. Write an algorithm to find minimal spanning tree using Krushkal’s algorithm. 7

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