



P.E.S. College of Engineering, Mandya - 571 401

(An Autonomous Institution affiliated to VTU, Belagavi)

First Semester, M.Tech. - Civil Engineering (MCAD)

Semester End Examination; April / May - 2021

Computational Structural Mechanics and FEM

Time: 3 hrs

Max. Marks: 100

Course Outcomes

The Students will be able to:

CO1: Analyze and find the complexity of the given problem.

CO2: Design efficient algorithm using Divide-and-Conquer Strategy.

CO3: Design and analyze algorithms to optimization problems.

CO4: Compute optimal solution for the problem using approximation algorithms.

CO5: Apply randomized algorithms for the given problem.

Note: I) Answer any **FIVE** full questions, selecting **ONE** full question from each unit.

II) Any **THREE** units will have internal choice and remaining **TWO** unit questions are compulsory.

III) Each unit carries 20 marks. **IV)** Missing data, if any, may suitably be assumed.

Q. No.	UNIT - I	Marks	BLs	COs	POs
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- 1a. Analyze the pin jointed truss shown in Fig. 1(a). Using direct stiffness method, determine displacement of joint 1 and forces in members. Take $A = 1000 \text{ mm}^2$, $E = 3 \times 10^5 \text{ N/mm}^2$.

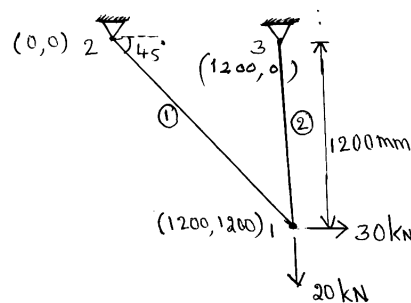


Fig. 1(a)

20 L3 CO1 PO2,3

OR

- 1d. What are the difference between stiffness and flexibility method?
- 1e. The top and bottom surfaces of the continuous beam as shown in Fig.1(e) are heated 20°C and 40°C respectively. Compute the displacement and element stress resultant. Using direct stiffness approach. Take $E = 200 \text{ GPa}$, $\alpha = 1.2 \times 10^{-5} / ^\circ\text{C}$

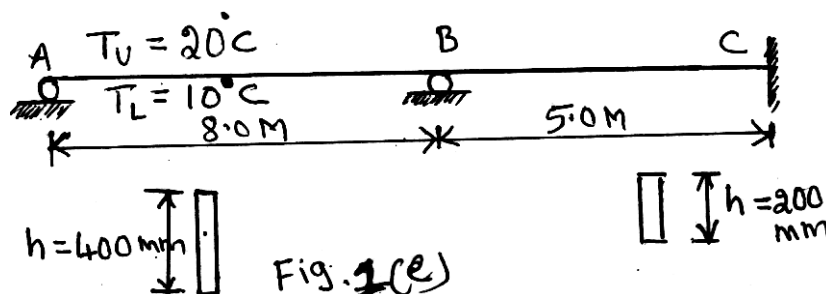
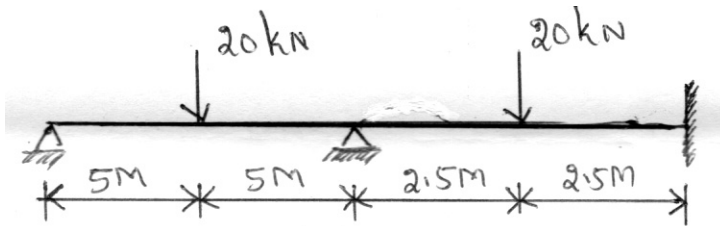


Fig. 1(e)

12 L3 CO2 PO2

UNIT - II

- 2 a. Determine the member forces for the continuous beam shown in Fig. 2(a). Using direct stiffness method. Draw BMD and SFD. Take $EI = \text{constant}$.



20 L3 CO2 PO3

Fig. 2(a)

UNIT - III

- 3 a. Derive the deflection equation for a simply supported beam subjected to UDL $w/\text{unit length}$ using Galerkin's method. Also calculate maximum deflection at the centre and compare the exact value of deflection.
- 3 b. Explain the convergence requirements.

15 L3 CO3 PO2

5 L2 CO3 PO2

OR

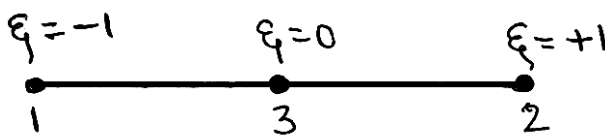
- 3 d. Discuss briefly the various steps of finite element formation.
- 3 e. Explain briefly with example;
- i) Higher order elements and Lower order element
 - ii) Natural coordinate and Area coordinate

12 L2 CO3 PO1

8 L2 CO3 PO1

UNIT - IV

- 4 a. Derive the shape function $[N]$, strain displacement matrix $[B]$ and element stiffness matrix $[k]$ for a three noded one dimensional bar element with natural coordinate system as shown in Fig. 4(a).

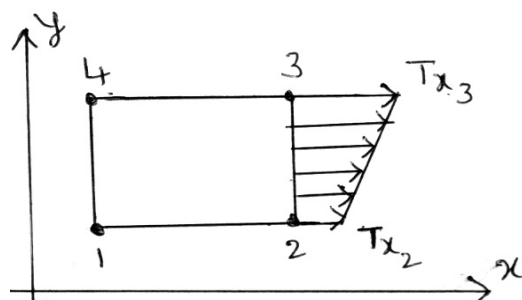


20 L3 CO4 PO2

Fig. 4(a)

OR

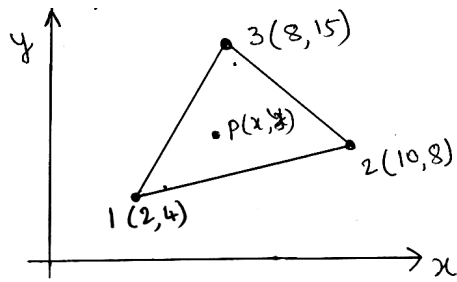
- 4 d. Derive the nodal load vector due to surface traction for the rectangular element as shown in Fig.4(d).



14 L3 CO4 PO2

4 e. Evaluate the shaper function for the CST element as shown in Fig. 4(e)

$$p(x, y) = p(5, 10).$$



6 L3 CO4 PO2

Fig. 4(e)

UNIT - V

5 a. Derive the shape function for the two noded Euler Bernoulli beam element and plot their shapes.

12 L3 CO4 PO2

5 b. Evaluate the following integral, using Gauss two sampling point formula and verify the exact value.

8 L3 CO4 PO1

$$I = \int_0^1 \frac{1}{(1+x^2)} dx$$

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