



P.E.S. College of Engineering, Mandya - 571 401

(An Autonomous Institution affiliated to VTU, Belagavi)

First Semester, M.Tech. - Civil Engineering (MCAD)

Semester End Examination; April / July -2021

Reliability Analysis and Design of Structural Elements

Time: 3 hrs

Max. Marks: 100

Course Outcomes

The Students will be able to:

CO1: Apply statistical principles for analyzing randomness in variables.

CO2: Test goodness of fit of distribution in the data.

CO3: Adopt different acceptance and rejection tests for strength and other parameters of measurements.

CO4: carry out reliability analysis and compute reliability index for the given design details.

Note: I) Answer any **FIVE** full questions, selecting **ONE** full question from each unit.

II) Any **THREE** units will have internal choice and remaining **TWO** unit questions are compulsory.

III) Each unit carries 20 marks. **IV)** Missing data, if any, may suitably be assumed.

V) Use of statistical tables allowed.

Q. No.	UNIT - I	Marks	BLs	COs	POs																						
1 a.	<p>The following are the results obtained in an experiment. Calculate the mean, standard deviation and coefficient of variation. Plot a histogram. Determine the chance of getting a value less than 6.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>2</td><td>7</td><td>9</td><td>10</td><td>20</td><td>21</td><td>22</td><td>13</td><td>14</td><td>13</td><td>19</td><td>26</td><td>28</td><td>15</td><td>16</td> </tr> </table>	2	7	9	10	20	21	22	13	14	13	19	26	28	15	16	10	L4	CO1	PO1,2							
2	7	9	10	20	21	22	13	14	13	19	26	28	15	16													
b.	<p>Calculate the correlation coefficient between X and Y for the following data. What do you infer?</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td><td>5</td><td>15</td><td>18</td><td>20</td><td>25</td><td>25</td><td>30</td><td>34</td><td>38</td><td>50</td> </tr> <tr> <td>y</td><td>45</td><td>32</td><td>37</td><td>33</td><td>24</td><td>29</td><td>26</td><td>22</td><td>24</td><td>15</td> </tr> </table>	x	5	15	18	20	25	25	30	34	38	50	y	45	32	37	33	24	29	26	22	24	15	10	L4	CO1	PO1,2
x	5	15	18	20	25	25	30	34	38	50																	
y	45	32	37	33	24	29	26	22	24	15																	
OR																											
1 d.	<p>List the properties of;</p> <p>i) Normal distribution ii) Log normal distribution</p>	10	L1	CO1	PO1,2																						
e.	<p>The mean strength of weld is 1.2 kN/mm² and its standard deviation is 0.4 kN/mm². If the weld is designed for strength of 1.5 kN/mm², what is the probability of survival of the welds? If the weld follows:</p> <p>i) Normal distribution</p> <p>ii) Log normal distribution</p>	10	L4	CO1	PO1,2																						
UNIT - II																											
2 a.	<p>Fit a straight line for the following data:</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td><td>71</td><td>68</td><td>73</td><td>69</td><td>67</td><td>65</td><td>66</td><td>67</td> </tr> <tr> <td>y</td><td>69</td><td>72</td><td>70</td><td>70</td><td>68</td><td>67</td><td>68</td><td>64</td> </tr> </table>	x	71	68	73	69	67	65	66	67	y	69	72	70	70	68	67	68	64	10	L4	CO2	PO1,2				
x	71	68	73	69	67	65	66	67																			
y	69	72	70	70	68	67	68	64																			

- b. Find the least square polynomial approximation of degree two for the following data:

10 L4 CO2 PO1,2

x	0	1	2	3	4
y	-4	-1	4	11	20

UNIT - III

- 3 a. A simply supported beam of span 'l' is under a uniformly distributed load of 10 kN/m. Establish the statistics of maximum bending moment. Given: $l = N(5.3, 0.2) m$ and $W = N(25.5, 5.7) kN/m$.

10 L4 CO3 PO1,2

- b. A Cantilever beam of span 'l' is subjected to a point load 10 kN at the free end. Establish the statistics of maximum deflection. Given; $W = N(20, 5) kN$, $l = N(2.7, 0.1) m$, $E = N(2 \times 10^5, 0.2 \times 10^5) N/mm^2$ $I = N(5400 \times 10^6, 270 \times 10^6) mm^4$

10 L4 CO3 PO1,2

UNIT - IV

- 4 a. A steel beam, whose cross section is classified as a compact section, this implies that its moment carrying capacity is the plastic moment computed as $M_p = f_y \times Z$, where Z =plastic section modulus and f_y = yield strength. The total load effect is denoted by M , which is the maximum moment demand on the beam due to the applied loading. The strength limit state function is $g(x) = f_y.Z - M$. Solve the problem by FOSM method and compute;

10 L4 CO4 PO1,2

- i) Reliability index ii) The risk or Probability of failure

Given;

Variable	Mean	Standard deviation
f_y	275.8 N/mm ²	34.475 N/mm ²
Z	819353.2 mm ³	40967.66 mm ³
M	1.1298×10^8 N-mm	22.596×10^6 N-mm

- b. A tension element of circular cross section subjected to external load. The limit state function $g(x) = f_y.A - P$. Solve the problem by FOSM method compute the reliability index, probability of success and probability of failure. Given;

10 L4 CO4 PO1,2

Variable	Mean	Standard deviation
Load $P(N)$	2.6689×10^4	1.7774×10^3
Yield $f_y (N/mm^2)$	1.0755×10^9	2.9576×10^7
Diameter $d(m)$	0.5842×10^{-2}	0.0759×10^{-3}

OR

4 d. Determine the reliability index of a simply supported beam of span ‘*l*’ subjected to uniformly distributed load *w/m* at the limit state of flexure. The failure surface is given by,

$$g(x) = f_y \cdot Z - \frac{wl^2}{8}. \text{ Solve the problem by Hasofer-lind method.}$$

Perform one complete iteration. Given;

20 L4 CO4 PO1,2

Variable	Mean	Standard deviation
Characteristic f_y strength $N(\text{mm}^2)$	272.41	13.62
Section modulus $Z(\text{mm}^3)$	3662.48×10^3	366248
Load w (N/m)	20.052	3.008
Span L (mm)	7082.54	354.13

UNIT - V

5 a. The strength of an axially loaded short column is given by $R = 0.67C.A_c + A_s.F$. Where C is the cube strength of concrete. F is the yield strength of steel. A_c is the area of steel. Generate the statistics of R (10 values). Compare the values with the theoretical values also find the percentage error. Given;

20 L4 CO4 PO1,2

Variable	Mean	Standard deviation
$C(\text{N}/\text{mm}^2)$	19.54	4.1
$F(\text{N}/\text{mm}^2)$	469	46.9
A_c (mm^2)	125000	-
A_s (mm^2)	1250	-

OR

5 d. The strength of an axially loaded column is given by $R = A_c .c + A_s F$ Where C is the cube strength of concrete. F is the yield strength of steel. A_c is the area of concrete and A_s is the area of steel. The column is subjected to an axial load $Q = N$ (1800, 540) kN. Generate the statistics of R and S (10 values) count the number of failures. Also find probabilities of failure. Given;

20 L4 CO4 PO1,2

Variable	Mean	Standard deviation
$C(\text{N} /\text{mm}^2)$	19.5	4.1
$F(\text{N}/\text{mm}^2)$	485	50
A_c (mm^2)	135000	500
A_s (mm^2)	1250	25

* * *