



**P.E.S. College of Engineering, Mandya - 571 401**

(An Autonomous Institution affiliated to VTU, Belagavi)

**Fourth Semester, B.E. - Computer Science and Engineering**

**Semester End Examination; July/August - 2022**

**Theory of Computation**

Time: 3 hrs

Max. Marks: 100

Note: I) PART - A is compulsory. Two marks for each question.

II) PART - B: Answer any Two sub questions (from a, b, c) for a Maximum of 18 marks from each unit.

Q. No.	Questions	Marks
<b>I : PART - A</b>		<b>10</b>

- |      |  |   |
|------|--|---|
| I a. | Define DFA.  | 2 |
| b.   | Define Regular Expression.                                 | 2 |
| c.   | Write CFG for the CFL $L = \{a^n b^{2n} \mid n \geq 0\}$ . | 2 |
| d.   | Define DPDA.   | 2 |
| e.   | Define TM.   | 2 |

<b>II : PART - B</b>		<b>90</b>
<b>UNIT - I</b>		<b>18</b>

- |      |  |   |
|------|--|---|
| 1 a. | Design a DFA to recognise all the strings, over $\Sigma = \{a, b\}$ , which ends with 'aba'.           | 9 |
| b.   | Convert the following NFA into its equivalent DFA and hence state the language recognised by the same. | 9 |

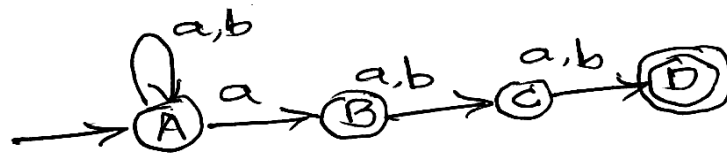


Fig Q1(b)

- |    |  |   |
|----|--|---|
| c. | Convert the following $\epsilon$ -NFA into its equivalent DFA and hence state the language recognised by the same. | 9 |
|----|--|---|



Fig Q1(c)

<b>UNIT - II</b>		<b>18</b>
------------------	--	-----------

- |      |   |   |
|------|---|---|
| 2 a. | Write regular expression for the following regular languages over $\Sigma = \{a, b\}$ |   |
| i)   | Ends with either <i>abb</i> or <i>aba</i> or <i>aab</i>                               | 9 |
| ii)  | $L = \{a^i b^j \mid (i+j) \text{ is even}\}$  |   |
| iii) | $ W  \bmod 3 = 2$   |   |

- b. State and prove pumping lemma for regular languages. 9
- c. Prove that for every regular expression  $R$ , representing the regular language  $L(R)$ , there is an equivalent DFA  $M$  such that  $L(M) = L(R)$ . 9

**UNIT - III****18**

3 a. Write CFG for the following CFLs:

i)  $L = \{a^i b^j c^k \mid i = j \text{ or } j = k \text{ or } k = i\}$

ii)  $L = \{a^i b^j c^k \mid i = 3(j + k)\}$

iii) Palindrome over  $\Sigma = \{a, b\}$

- b. Define ambiguous grammar and hence prove that the following grammar is ambiguous 9  
 $E \rightarrow E + E \mid E * E \mid id$
- c. Convert the given CFG into its equivalent PDA 9  
 $E \rightarrow E + E \mid E * E \mid id$

**UNIT - IV****18**

4 a. Design PDA for the following CFL  $L = \{a^i b^j c^k \mid i = j + k\}$

- b. Design PDA to recognise the CFL,  $L = \{W \in \{a, b\}^* \mid n_a(W) = n_b(W)\}$ . State whether the resultant PDA is DPDA/NPDA. Justify your answer. 9
- c. Define PDA, Instantaneous description a PDA and language accepted by PDA. 9

**UNIT - V****18**

5 a. Design TM to recognize the language  $L = \{a^n b^n c^n \mid n \geq 0\}$

- b. Explain any two extensions of TM. 9
- c. Explain recursively enumerable languages and post's correspondence problem. 9

\* \* \* \*