



# P.E.S. College of Engineering, Mandya - 571 401

(An Autonomous Institution affiliated to VTU, Belagavi)

Fourth Semester, B.E., - Information Science and Engineering

Semester End Examination; August - 2023

Finite Automata and Formal Languages

Time: 3 hrs

Max. Marks: 100

## Course Outcomes

The Students will be able to:

CO1: Construct regular expression and finite automata

CO2: Analyze regular Language

CO3: Design context free grammars

CO4: Design push down automata

CO5: Design Turing machine

**Note:** I) PART - A is compulsory. Two marks for each question.

II) PART - B: Answer any **Two** sub questions (from a, b, c) for a Maximum of **18 marks** from each unit.

Q. No.	Questions	Marks	BLs	COs
<b>I : PART - A</b>		<b>10</b>		
1 a.	Define regular expression.	2	L1	CO1
b.	Draw an NFA for the RE = $ab(a+b)^*$ .	2	L3	CO2
c.	Write a grammar to generate the following language: $L = \{a^n b^n \mid n \geq 1\}$	2	L3	CO3
d.	“Is there any need for pushdown automata when finite automata already exists?” Justify with answer.	2	L2	CO4
e.	Define Turing machine.	2	L1	CO5
<b>II : PART - B</b>		<b>90</b>		
<b>UNIT - I</b>		<b>18</b>		
2 a.	Define the following with an example: i) Alphabet    ii) String    iii) Kleen closure    iv) Language	9	L1	CO1
b.	Write a regular expression corresponding to each of the following subsets of $(a, b)^*$ i) The language of all strings in which the numbers of a's is odd ii) The language of all strings that do not end with ab iii) The language of all strings whose second symbol from the right end is a iv) $L = \{a^n b^m \mid n \geq 4, m \leq 3\}$	9	L3	CO1
c.	Design the DFA for the following language over $\Sigma = \{a, b\}$ i) $L = \{a W a \mid W \in (a, b)^*\}$ ii) Ending with ab or ba iii) Having even number of a's and odd numbers of b's	9	L3	CO1

UNIT - II

18

3 a. Convert the following NFA show in Fig.2.a to its equivalent DFA.

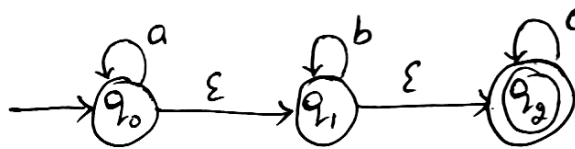


Fig. 2.a

9 L3 CO2

b. Prove that every R.E, There exists a FA which accepts the same language accepted by the R.E.

9 L2 CO2

c. Obtain a R.E for the FA shown in Fig .2(c), using Kleen's theorem.

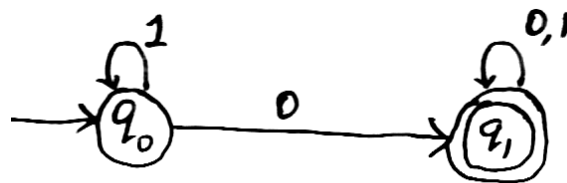


Fig. 2(c)

9 L3 CO2

UNIT - III

18

4 a. Construct a grammar for language representing strings of a's and b's

i) Having a substring ab

ii)  $L = \{ WW^R \mid W \in (a+b)^* \}$

4 L3 CO3

iii)  $L = \{ a^n b^{2n} \mid n, m \geq 1 \}$

iv)  $L = \{ a^{m+n} b^m c^n \mid n, m \geq 1 \}$

b. i) Consider the CFG with the following productions:

$E \rightarrow E^*T/T$

$T \rightarrow F-T/F$

$F \rightarrow (E) \mid a \mid b$

Write the leftmost derivation and rightmost derivation for the string

'a-((b\*a)-a)'

5 L3 CO3

ii) Show that the given grammar is ambiguous

$S \rightarrow aB \mid bA$

$A \rightarrow aS \mid bAA \mid a$

$B \rightarrow bs \mid aBB \mid b$

c. Convert the following CFG to CNF

$S \rightarrow ASB \mid \epsilon$

$A \rightarrow aAS \mid a$

$B \rightarrow SbS \mid A \mid bb$

9 L3 CO3

**UNIT - IV****18**

- 5 a. Construct a PDA to accept the language  $L = \{WCW^R \mid W \in (a+b)^*\}$  where  $W^R$  is reverse of  $W$  by a final state. 9 L3 CO4
- b. Construct a PDA to accept a string of balanced parentheses. The parentheses to be considered are  $(, [, ]$ . check whether the string  $[ ( ) ( [ ] )$  is accepted or rejected. 9 L3 CO4
- c. Is the PDA to accept the language  $L = \{W \mid W \in (a, b)^* \text{ and } n_a(W) > n_b(W)\}$  is deterministic? 9 L3 CO4

**UNIT - V****18**

- 6 a. i) Describe a Turing machine model. 4 L2
- ii) Construct a TM to accept the language  $L = \{\omega \mid \omega \in (0+1)^*\}$  containing the substring 001. 5 L3 CO5
- b. Draw a T.M to accept the language  $L = \{0^n 1^n \mid n \geq 1\}$ . 9 L3 CO5
- c. Explain how to combine more than one TM with an example. 9 L2 CO5

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