

**P.E.S. College of Engineering, Mandya - 571 401***(An Autonomous Institution affiliated to VTU, Belagavi)***Fourth Semester, B.E. - Information Science and Engineering****Semester End Examination; Sep. / Oct. - 2023****Theory of Computation**

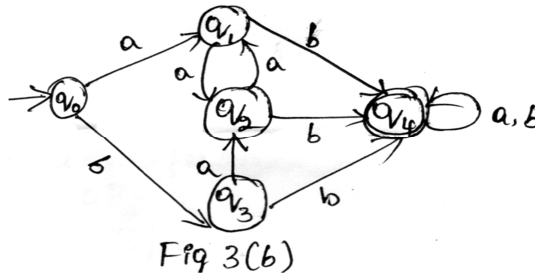
Time: 3 hrs

Max. Marks: 100

**Course Outcomes***The Students will be able to:**CO1: Understand the basic concept of Automata.**CO2: Apply the knowledge of Automata Theory for formal Languages**CO3: Analyze automata and their computational power to recognize languages**CO4: Design an automaton.***Note: I) PART - A is compulsory. Two marks for each question.****II) PART - B: Answer any Two sub questions (from a, b, c) for a Maximum of 18 marks from each unit.**

Q. No.	Questions	Marks	BLs	COs	POs																				
<b>I : PART - A</b>		<b>10</b>																							
1 a.	Write the applications of finite automata.	2	L2	CO1	PO1																				
b.	Write the applications of regular expressions.	2	L2	CO2	PO1																				
c.	Define Parse trees.	2	L1	CO3	PO1																				
d.	Define PDA.	2	L1	CO2	PO1																				
e.	Explain Turing machine model.	2	L2	CO1	PO1																				
<b>II : PART - B</b>		<b>90</b>																							
<b>UNIT - I</b>		<b>18</b>																							
2 a.	List out the differences between DFA, NFA and $\epsilon$ -NFA.	9	L2	CO1	PO																				
b.	Write DFA's for the following languages on $\Sigma = \{a, b\}$																								
	i) Set of all strings ending with $ab$	9	L2	CO2	PO2																				
	ii) Set of all strings not containing the substring $aab$																								
	iii) Set of all strings having "Exactly one $a$ "																								
c.	Consider the following $\epsilon$ -NFA.																								
	<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td><math>\delta</math></td> <td><math>\epsilon</math></td> <td>a</td> <td>b</td> <td>c</td> </tr> <tr> <td>p</td> <td><math>\phi</math></td> <td>{p}</td> <td>{q}</td> <td>{r}</td> </tr> <tr> <td>q</td> <td>{p}</td> <td>{q}</td> <td>{r}</td> <td><math>\phi</math></td> </tr> <tr> <td>*r</td> <td>{q}</td> <td>{r}</td> <td><math>\phi</math></td> <td>{p}</td> </tr> </table>	$\delta$	$\epsilon$	a	b	c	p	$\phi$	{p}	{q}	{r}	q	{p}	{q}	{r}	$\phi$	*r	{q}	{r}	$\phi$	{p}	9	L3	CO4	PO2
$\delta$	$\epsilon$	a	b	c																					
p	$\phi$	{p}	{q}	{r}																					
q	{p}	{q}	{r}	$\phi$																					
*r	{q}	{r}	$\phi$	{p}																					
	i) Compute $\epsilon$ -closure of each state																								
	ii) Give all the strings of length three or less accepted by automata																								
	iii) Convert the automata to DFA																								
<b>UNIT - II</b>		<b>18</b>																							
3 a.	State and prove pumping lemma for regular languages show that the language $L = \{a^n b^n \mid n \geq 0\}$ is not regular.	9	L4	CO2	PO2																				

b. Minimize the following DFA:



9 L3 CO2 PO2

c. Write regular expression for the following language:

i)  $\{\omega \in \{a, b\}^* \text{ does not end with } ba\}$

9 L2 CO1 PO3

ii)  $\{\omega \in \{0, 1\}^* \text{ has substring } 001\}$

iii)  $\{\omega \in \{0, 1\}^* \mid |\omega| \text{ is even}\}$

**UNIT - III**

**18**

4 a. Consider the grammar:

$$S \rightarrow aS \mid aSbS \mid \epsilon$$

Is the above grammar ambiguous? Show that the string *aab* has two

9 L3 CO3 PO2

i) Parse trees

ii) Left most derivations

iii) Rightmost derivations

b. Convert the following grammar to CNF:

$$S \rightarrow 0A \mid 1B$$

$$A \rightarrow 0AA \mid 1S \mid 1$$

$$B \rightarrow 1BB \mid 0S \mid 0$$

9 L3 CO2 PO2

c. Obtain a CFG to generate the following language:

i)  $L = \{a^n b^{n+2} \mid n \geq 0\}$

9 L3 CO3 PO2

ii)  $L = \{\omega \omega^R \mid \omega \in \{a, b\}^*\}$

iii)  $L = \{0^m 1^m 2^n \mid m \geq 1 \text{ and } n \geq 0\}$

**UNIT - IV**

**18**

5 a. Obtain PDA from the following grammar:

$$S \rightarrow aABB \mid aAA$$

$$A \rightarrow aBB \mid a$$

$$B \rightarrow bBB \mid A$$

$$C \rightarrow a$$

9 L3 CO2 PO2

b. Design a PDA to accept the language

$L = \{\omega \mid \omega \in (a+b)^* \text{ and } n_a(\omega) = n_b(\omega)\}$  and is the PDA is deterministic

9 L4 CO4 PO2,3

c. Design a PDA to accept the language  $L = \{\omega \omega^R \mid \omega \in (a+b)^*\}$

9 L4 CO4 PO1,2,3

## UNIT - V

18

- 6 a. Obtain a Turing machine to accept the language  $L = \{0^n 1^n \mid n \geq 1\}$ . 9 L3 CO4 PO1,2
- b. Write short notes on the following:
- i) Multi-tape Turing machines 9 L2 CO1 PO1,2
  - ii) Non-deterministic Turing machine
  - iii) Undecidable problems
- c. Explain the following terms:
- i) Recursively Enumerable languages 9 L2 CO1 PO1,2
  - ii) Multi track Turing machine
  - iii) Post correspondence problem

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